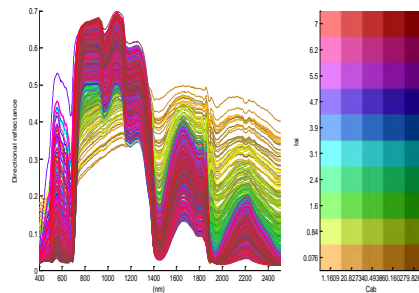
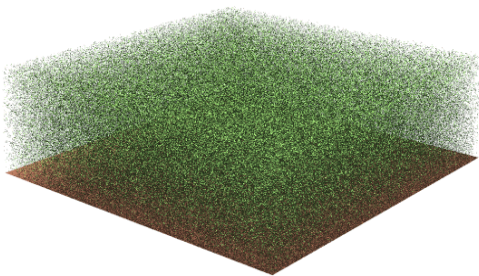


# From model simulations towards vegetation properties mapping:

*automating, optimizing & simplifying*



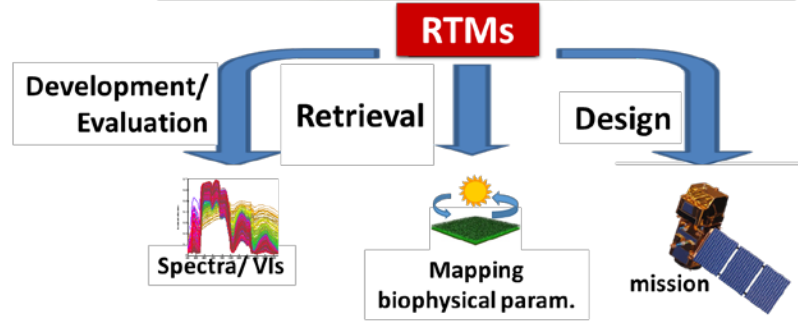
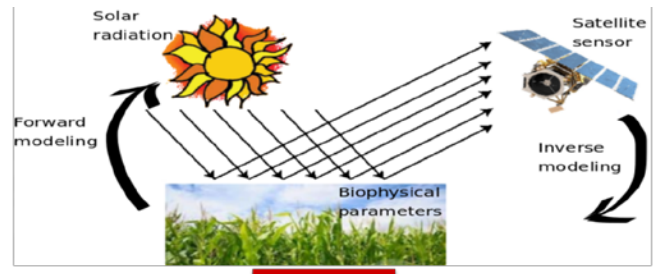
J. Verrelst, J.P. Rivera & J. Moreno

ISSI Workshop – 21-25 Nov2016

# Background

## AUTOMATING RTMs

- RTMs
- ARTMO/forward
- Retrieval toolboxes

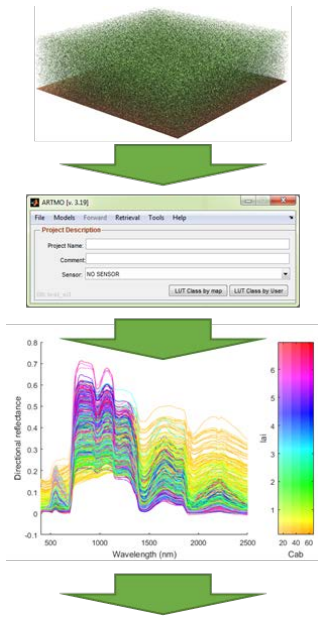


## OPTIMIZING exploiting spectroscopy data

- Retrieval
- Band selection
- Dimensionality & sample reduction

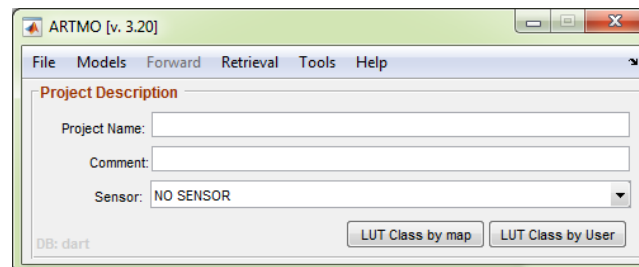
## SIMPLIFYING RTMs

- Global sensitivity analysis
- Emulation
- Retrieval



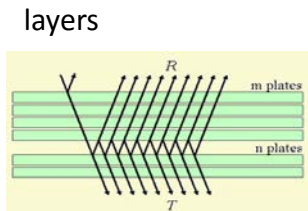
# AUTOMATING

- RTMs
- ARTMO/forward
- Retrieval toolboxes

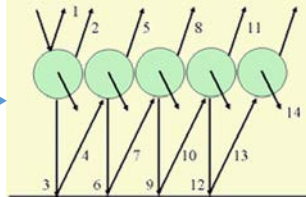


# Radiative transfer models (RTMs)

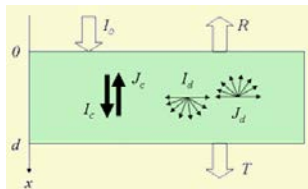
## Leaf RTMs



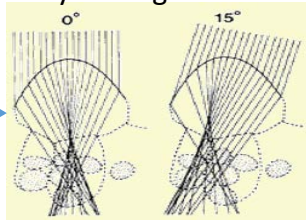
### Compact spheres



### N-fluxes



### Ray tracing



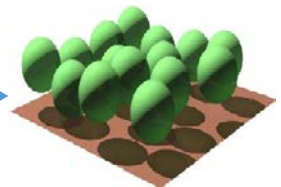
## Canopy RTMs



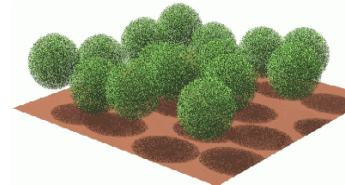
### Turbid medium



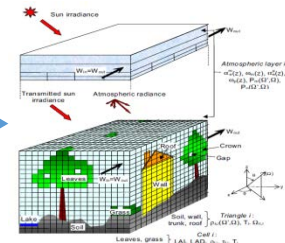
### Geometric



### Hybrid



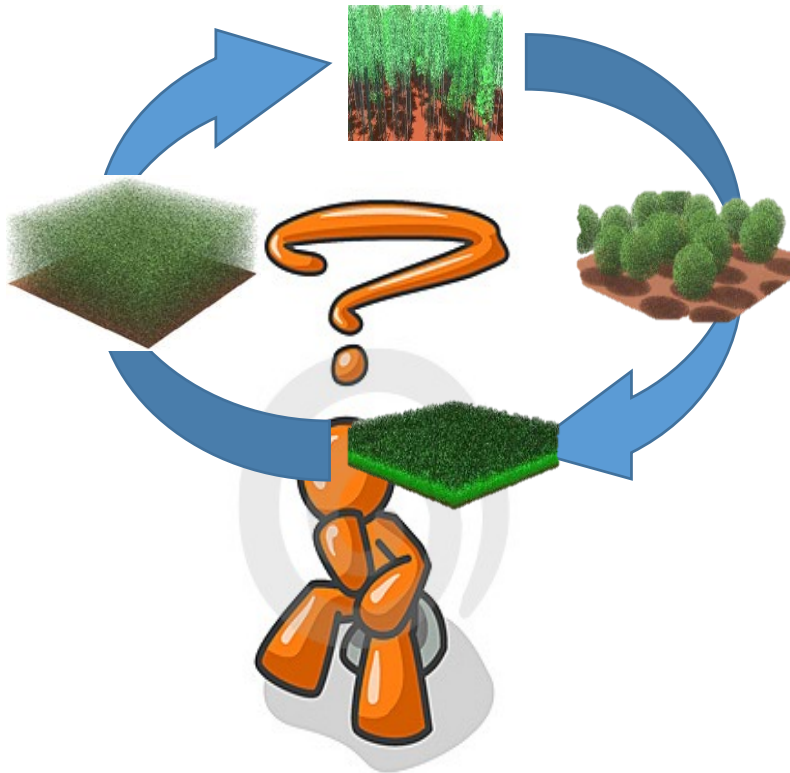
### Volumetric



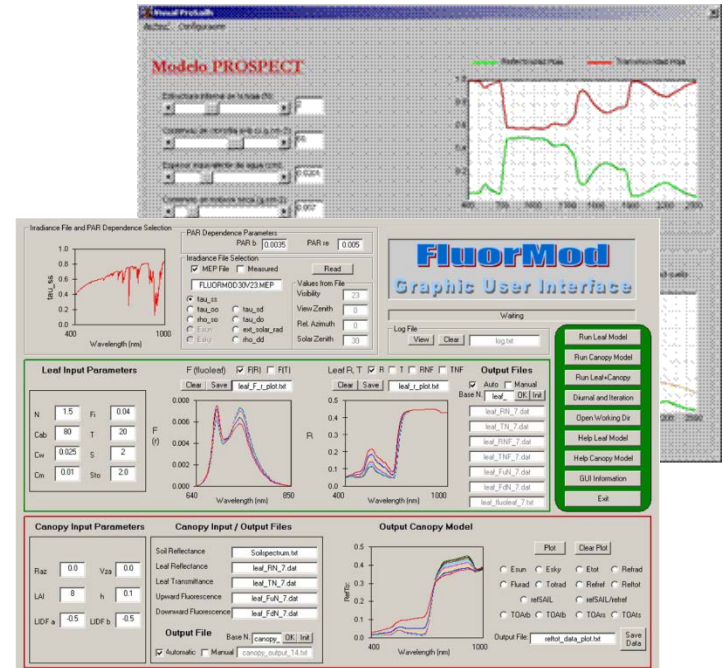
A diversity of RTMs exist with different complexity.

# RTMs are important tools in EO research, but not always easy to use. Only very few of them offer user-friendly interfaces.

## Which RTM to choose?



## Only very few offer a GUI.



- No interface exists that brings multiple RTMs together in one GUI.
- None of existing (publicly available) GUIs provide post-processing tools.

# Toolbox for EO applications:



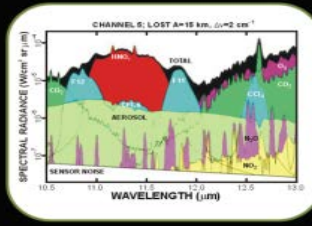
Automated  
Radiative  
Transfer  
Models  
Operator



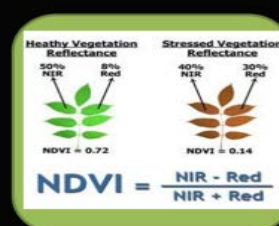
# ARTMO



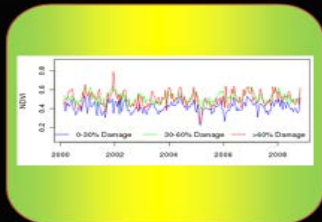
Atmospheric models



MODTRAN



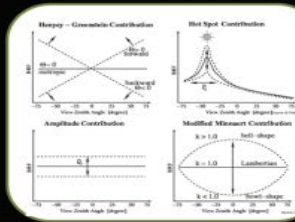
Vegetation indices



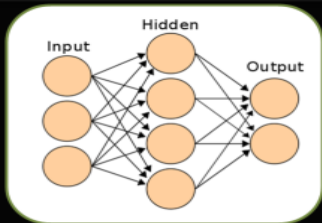
Time series analysis



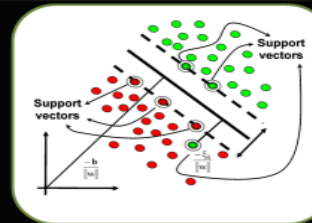
Ray tracing model



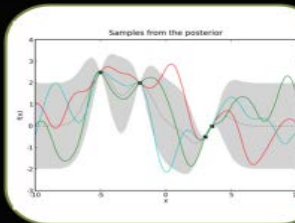
RPV model



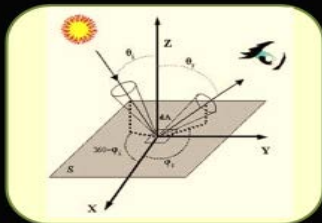
Neural nets



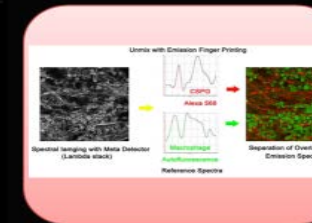
Support vectors



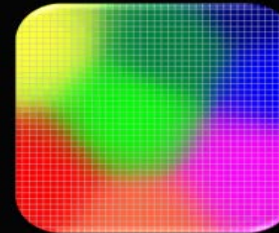
Gaussian Processes



BRDF apps

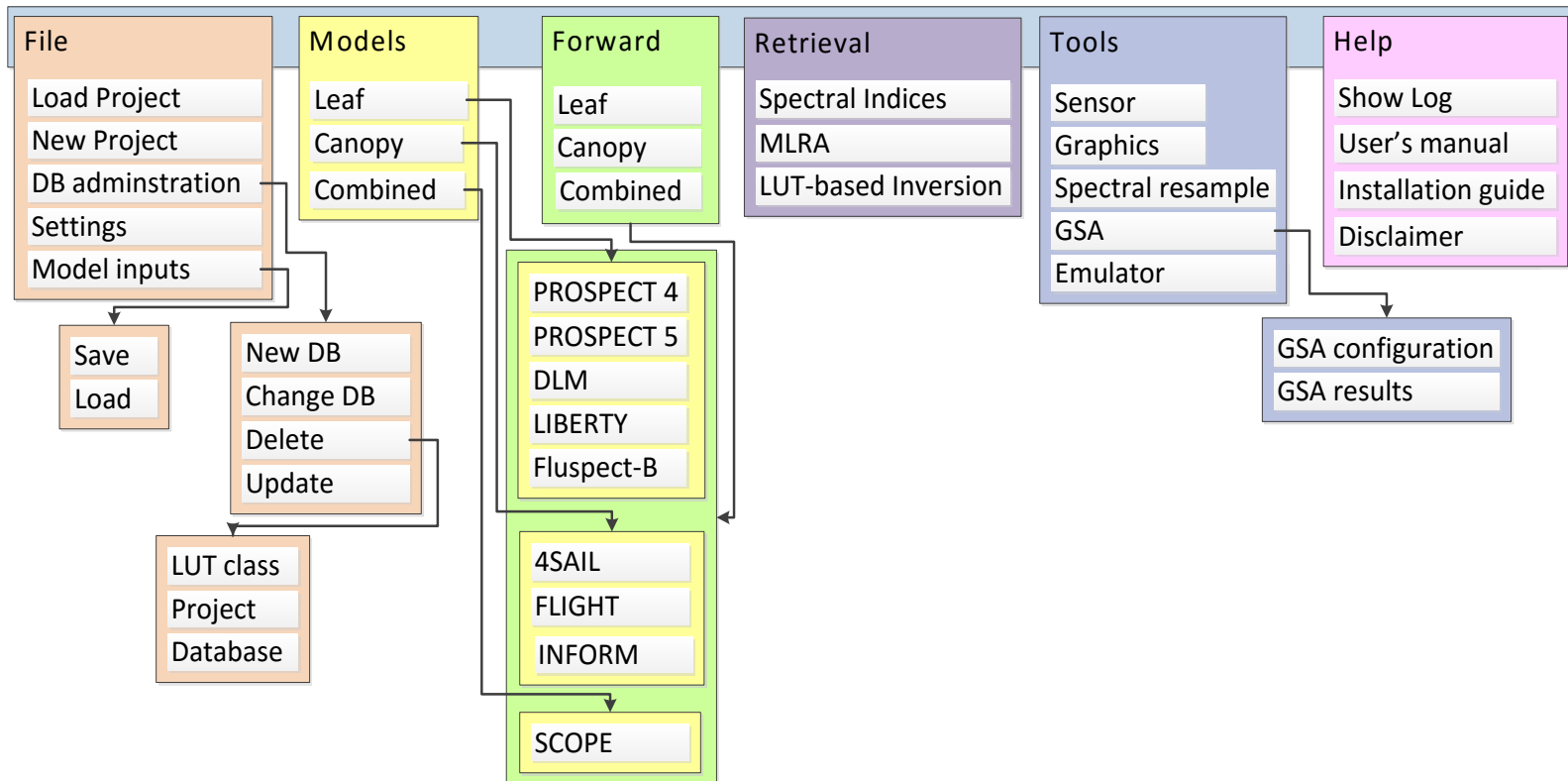
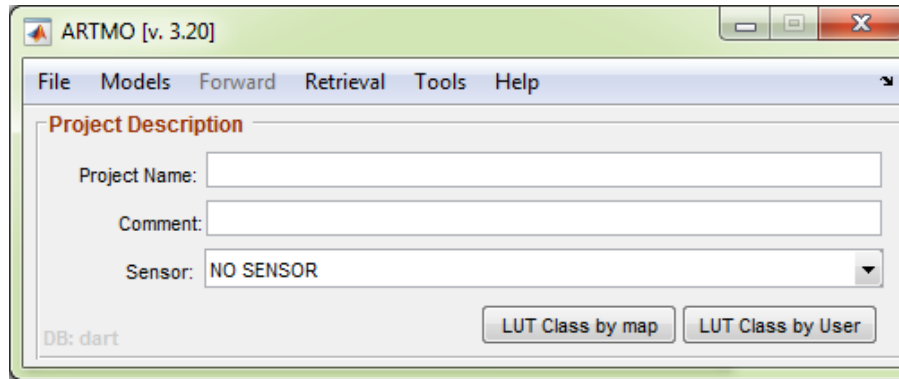
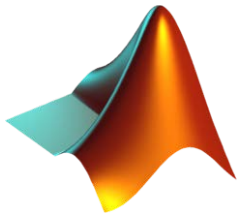


Spectral unmixing



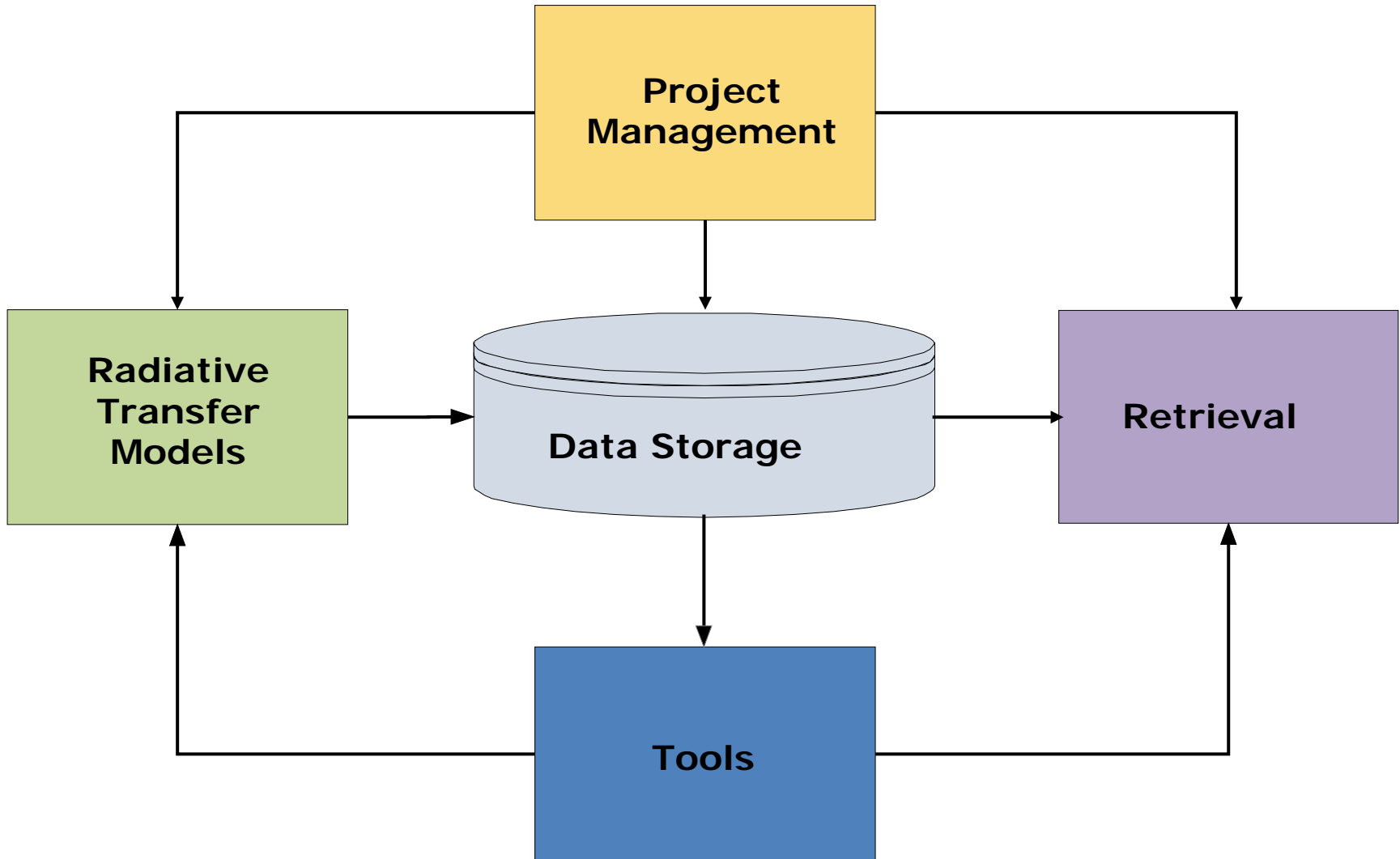
Classifiers

# ARTMO v. 3: modular design

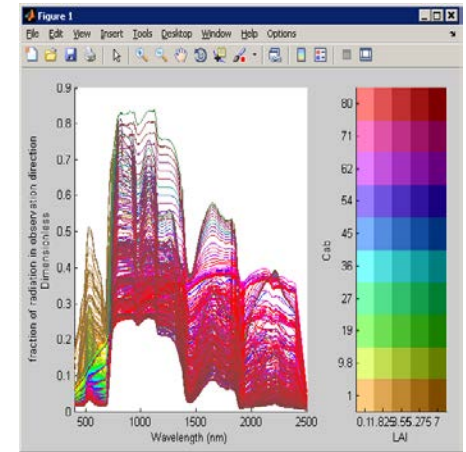
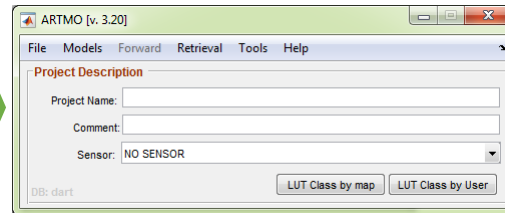
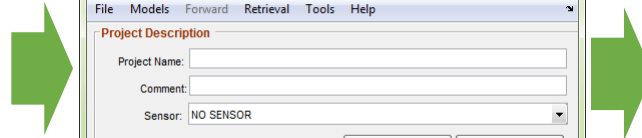
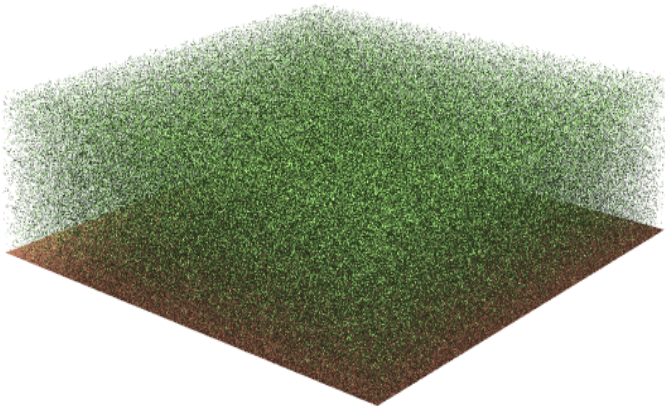




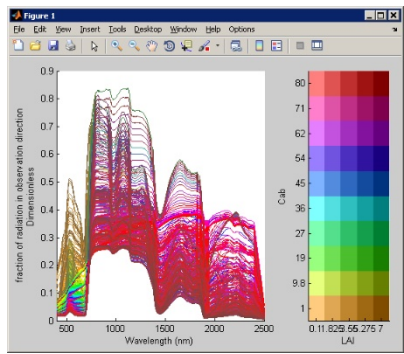
# Conceptual architecture ARTMO



# Forward



# RTM outputs only a few clicks away...



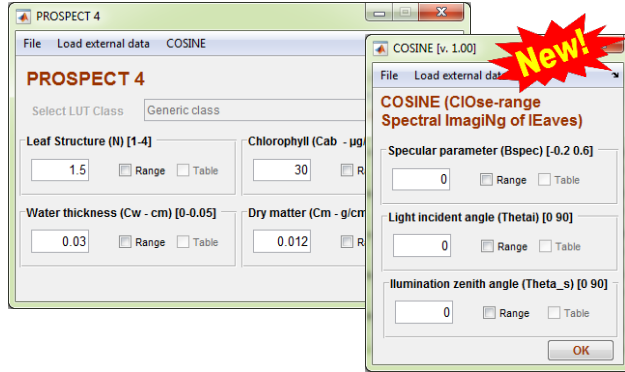

# Data flow

LUT Class	# Simulations	Subset
class1	2.0000e+09	10000

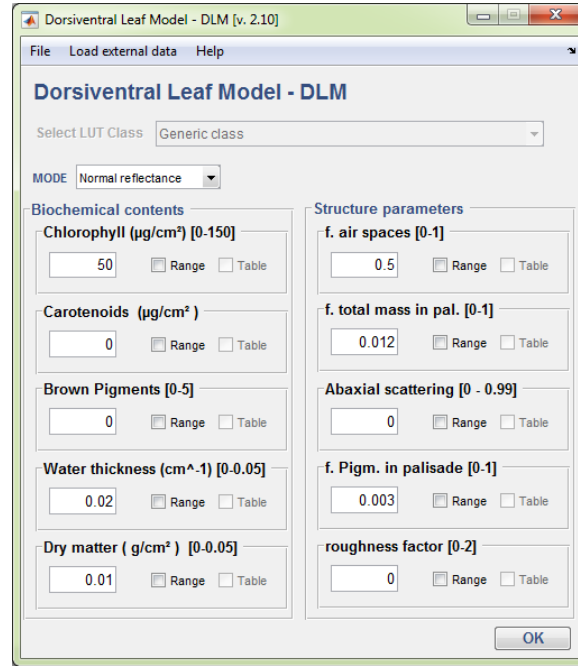
Radiative Transfer Models

# ARTMO's leaf models

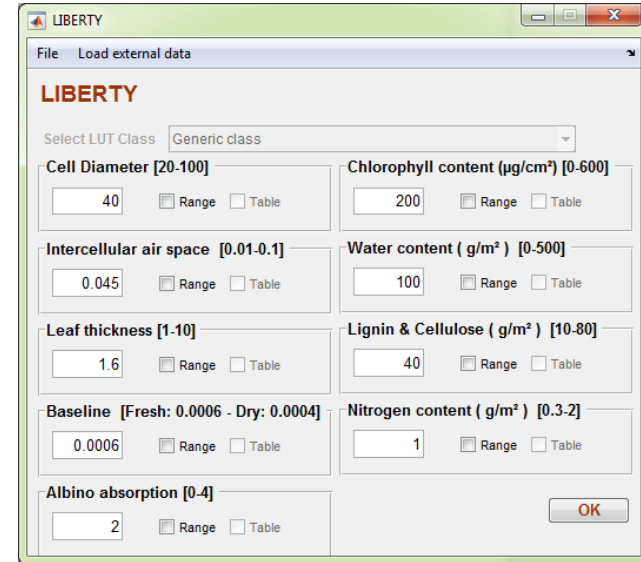
## PROSPECT-4



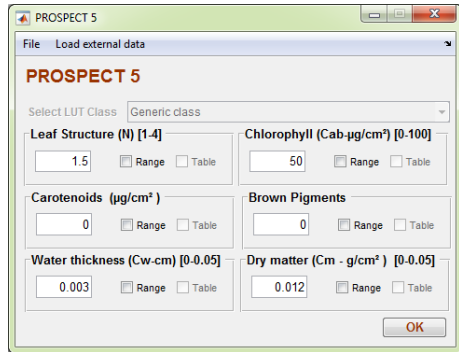
## DLM



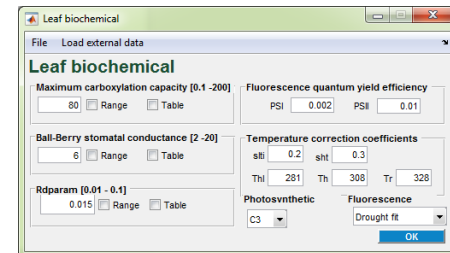
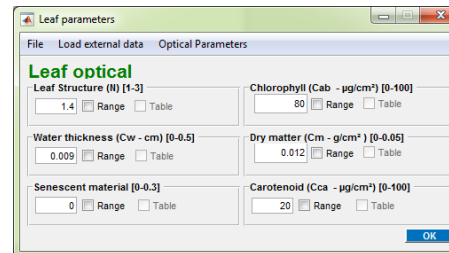
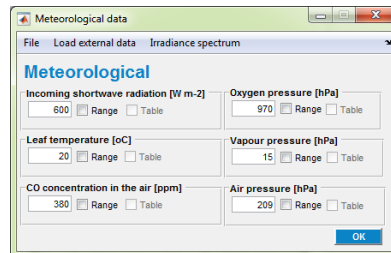
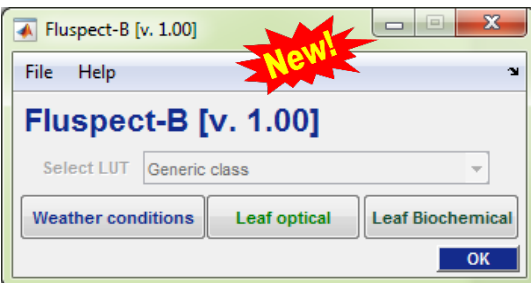
## LIBERTY



## PROSPECT-5



## Fluspect-B



# ARTMO's canopy models

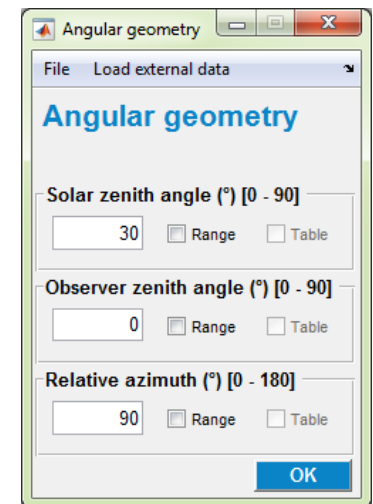
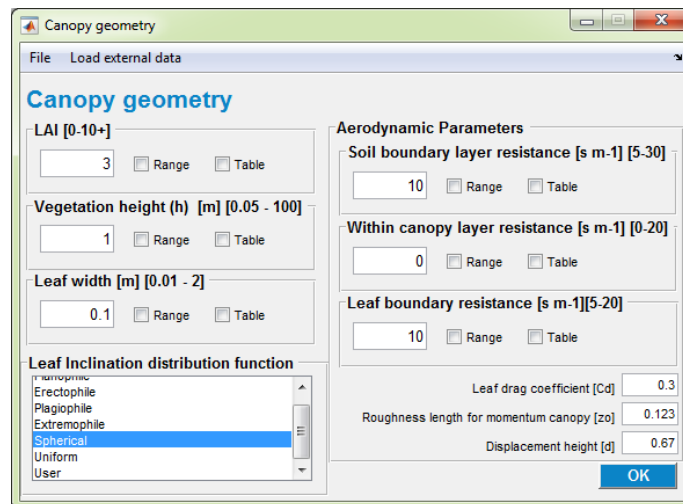
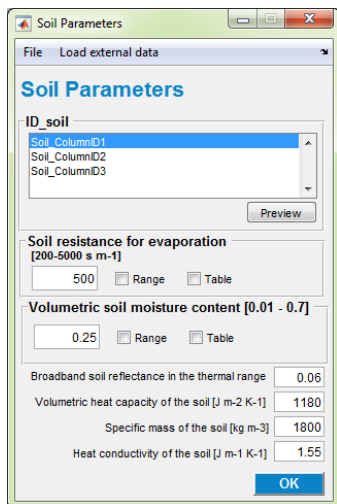
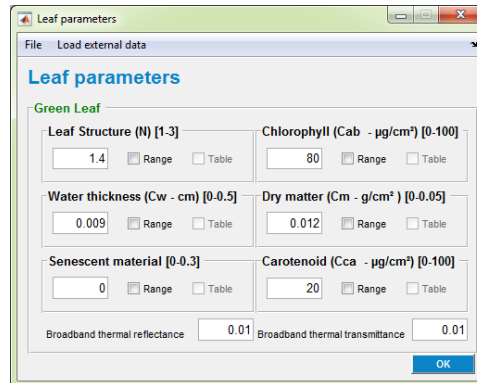
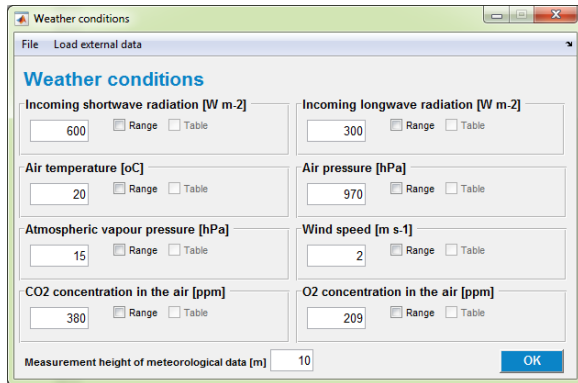
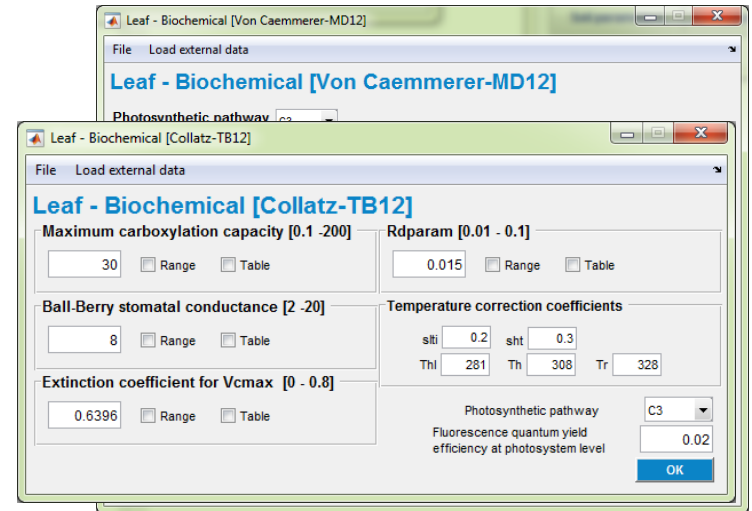
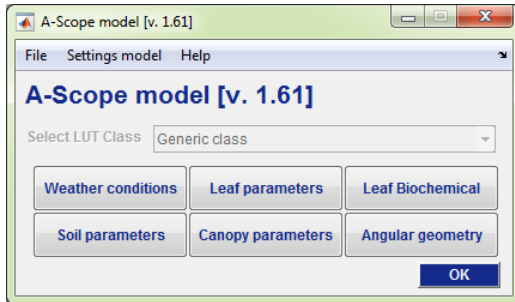
## SAIL

## INFORM

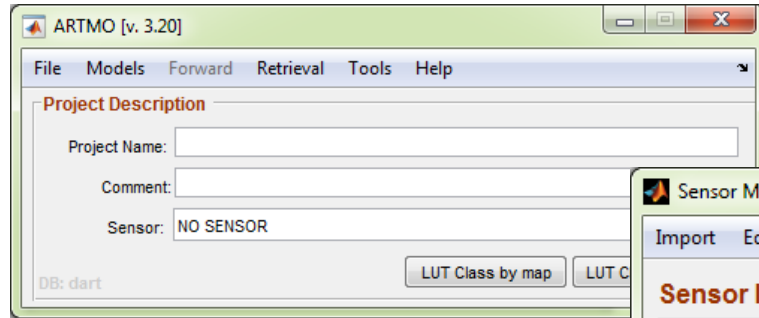
## FLIGHT

Radiative Transfer Models

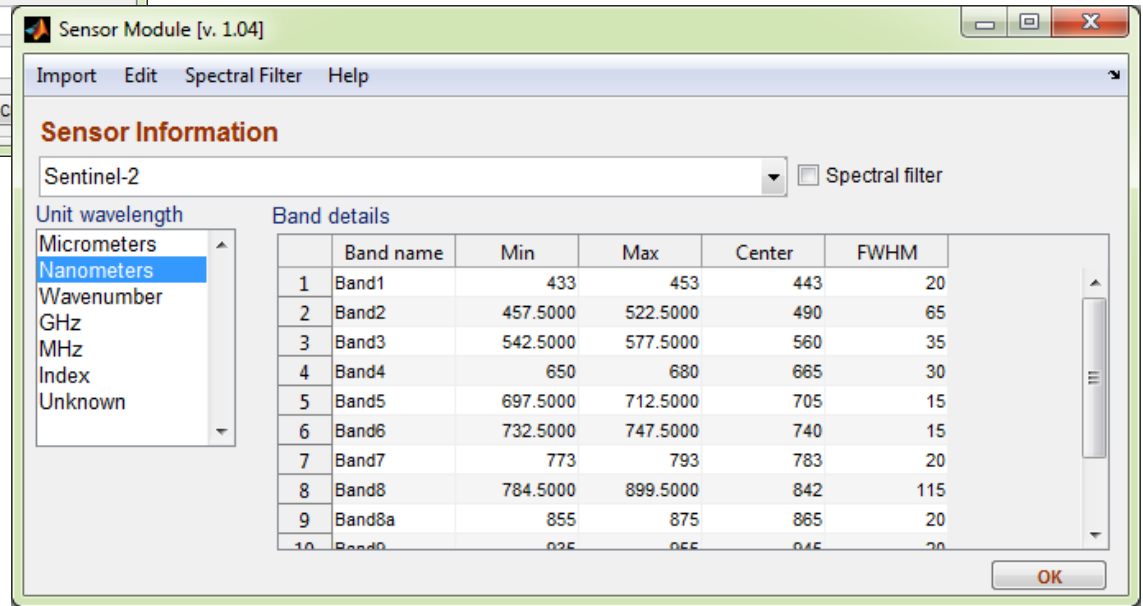
# ARTMO's combined models: SCOPE



# Sensor



*Simulations can be generated according to band settings of a selected sensor.*

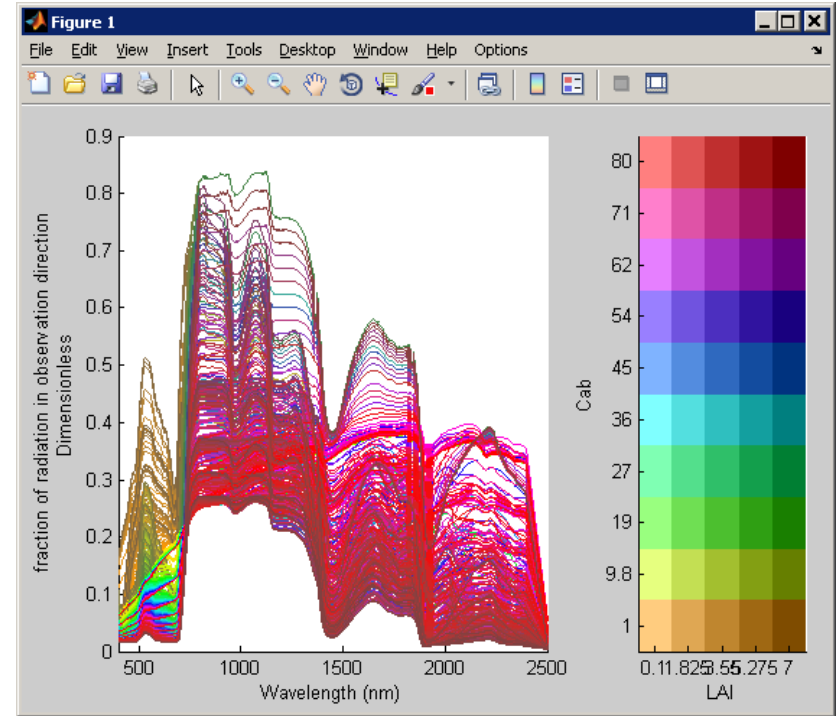
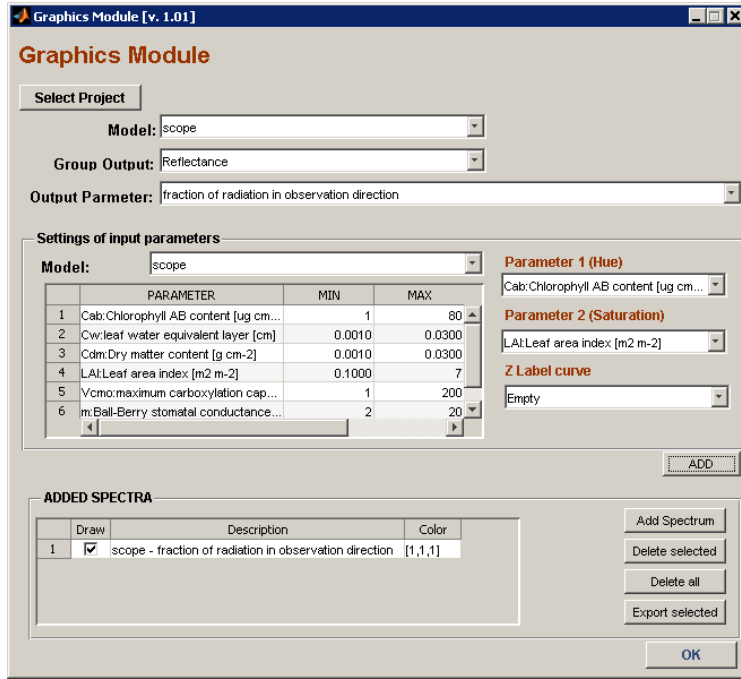


- New sensor settings can be imported by clicking on the **'Import'** button in the top bar.
- Existing band settings can be modified or new ones can be added by clicking on the **'Edit'** button.
- Also a spectral filter of a sensor can be imported or viewed by clicking on the **'Spectral Filter'** button.

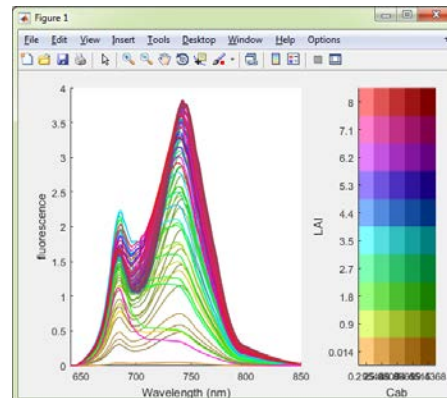
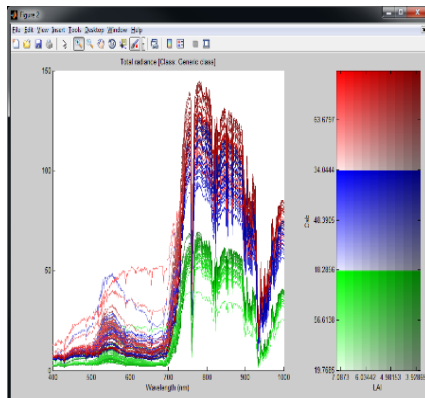
## Default sensors:

- Landsat 7 TM
- Landsat 7 ETM+
- SPOT-4 VMI
- SPOT-4 HRVIR
- CHRIS Mode-3
- MODIS
- MERIS
- Sentinel-2
- Sentinel-3 OLCI
- Sentinel-3 SLSTR
- Landsat 8
- Pleiades-1A
- Quickbird

# Graphics

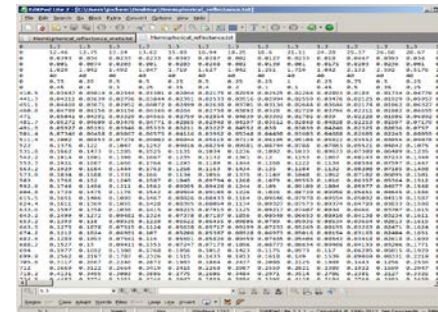


Visualization options:

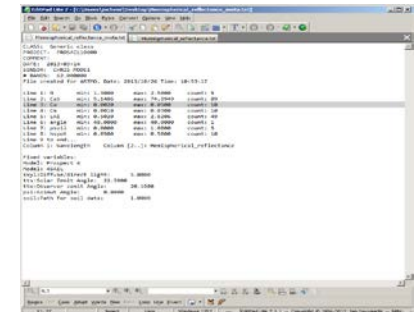


Export:

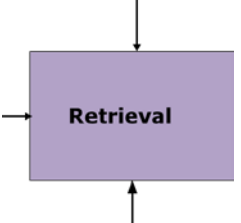
Spectral data



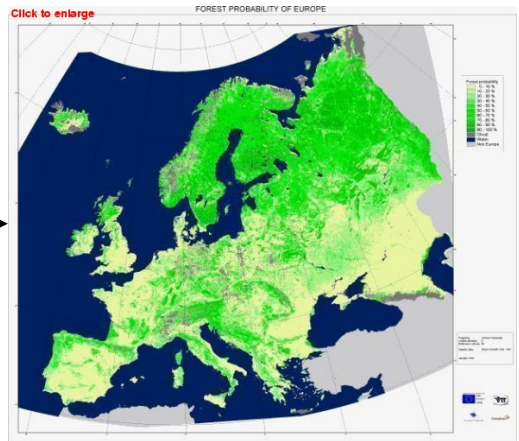
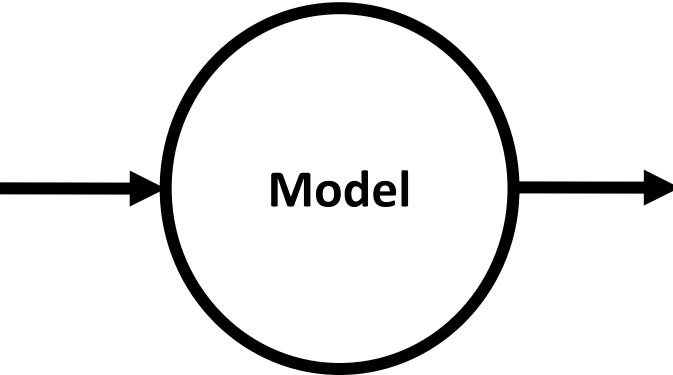
Associated metadata







# Retrieval



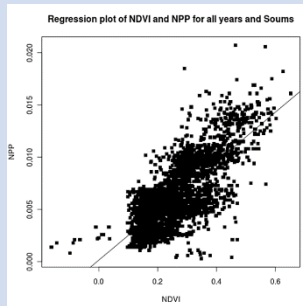
# Retrieval families

## Parametric regression

Spectral relationships that are sensitive to specific vegetation properties

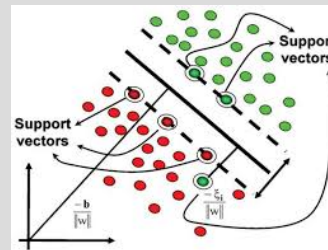
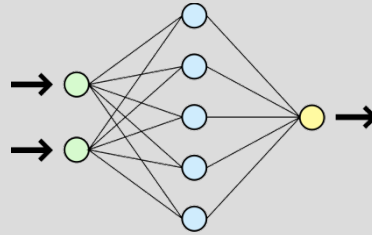
$$NDVI = \frac{(\rho_{NIR} - \rho_{RED})}{(\rho_{NIR} + \rho_{RED})}$$

Normalized Difference Vegetation Index



## Non-parametric regression

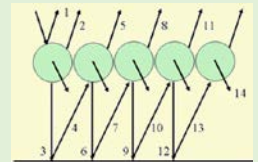
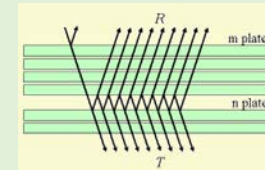
Advanced techniques that search for relationships between spectral data and biophysical variables



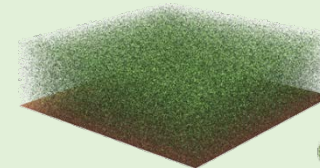
## RTM inversion

Models that simulate interactions between vegetation and radiation

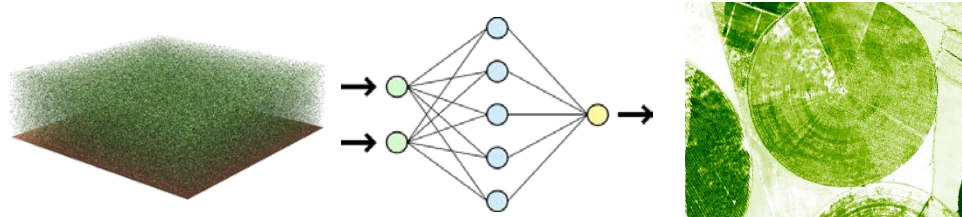
leaf



canopy

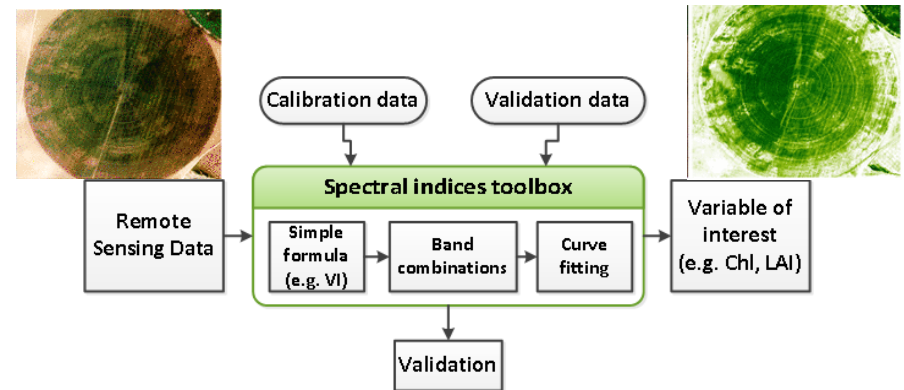
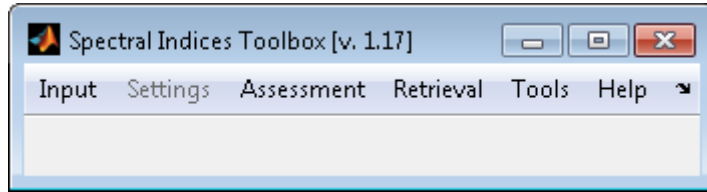


Methods of these different families can be combined: *hybrid methods*

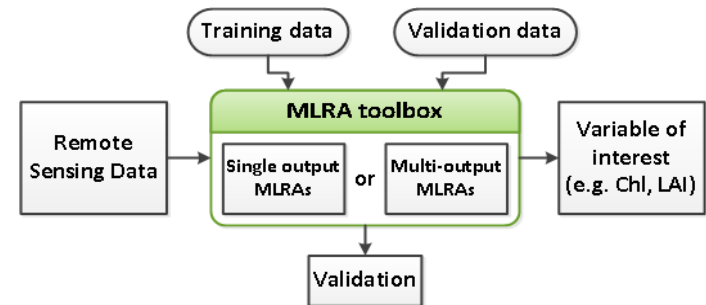
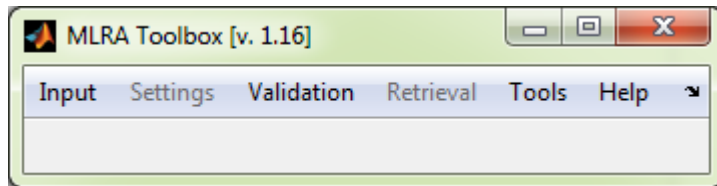


# ARTMO's retrieval toolboxes:

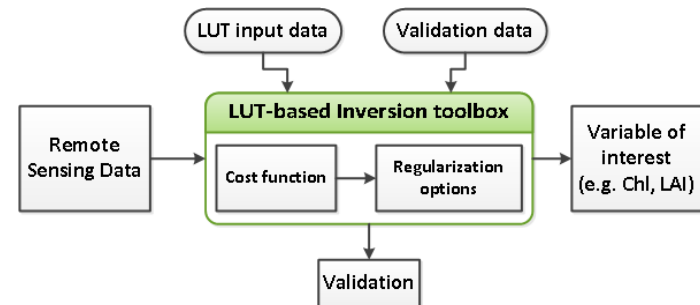
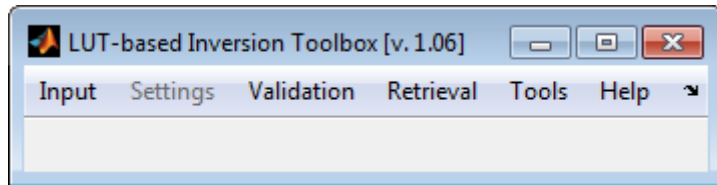
## Spectral indices toolbox



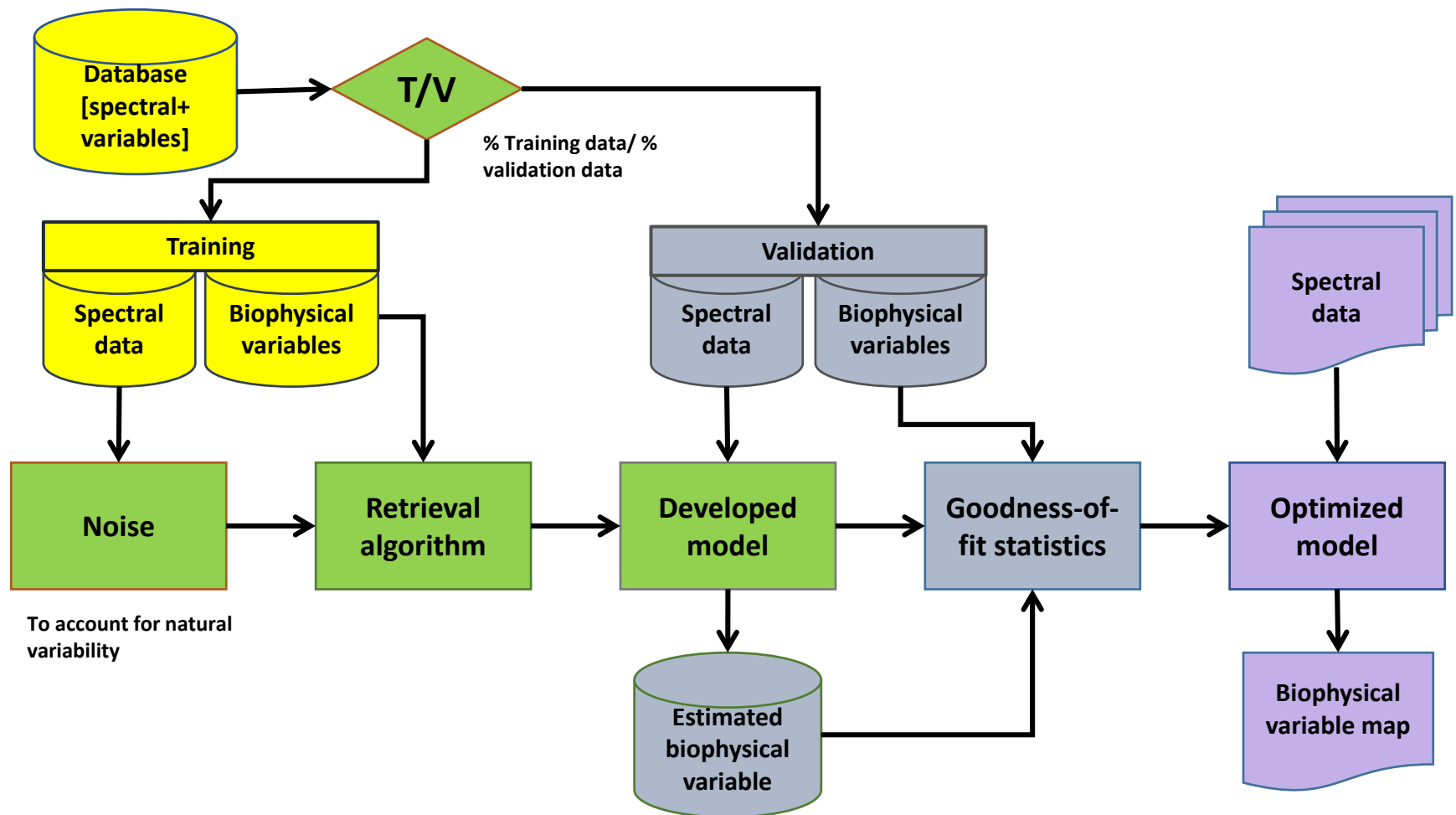
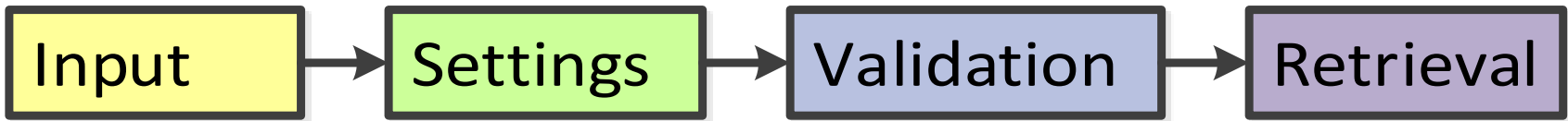
## Machine learning regression algorithm toolbox



## LUT-based inversion toolbox

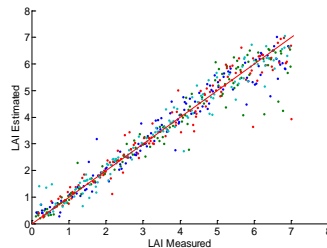


# General structure:

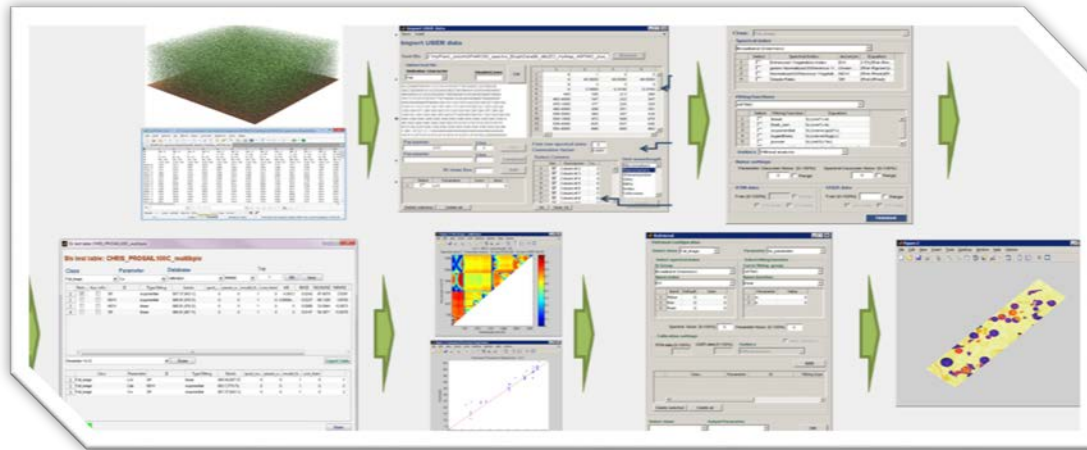
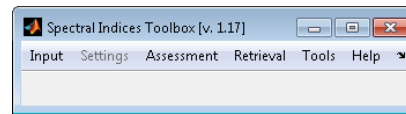


# OPTIMIZING

- Retrieval: parametric/non-parametric/inversion
- Band selection
- Dimensionality & sample reduction



# Spectral indices toolbox:



## Properties:

- Calculates all possible band combinations.
- For index formulations with up to 10-band indices ( $\#b^{10}$ , for a 10-band sensor that would be 10 billion combinations)
- Includes multiple fitting functions (linear, exponential, logarithmic, power, polynomial)
- Noise & Cross-validation options
- Results stored in MySQL
- Top-performing indices per formulation and fitting function are given.
- Can process both image or individual spectra.

**SI Settings**

Class: Full\_image

**Spectral index**

Broadband Greenness

Select	Spectral Index	Acron...	Equation
<input type="checkbox"/>	Enhanced Vegetation Index	EVI	$2.5 * ((R_{nir} - R_{red}) / (R_{nir} + R_{red}))$
<input type="checkbox"/>	green Normalized Difference V... Green ...	( $R_{nir} - R_{green}$ ) / ...	
<input type="checkbox"/>	Normalized Difference Vegetat... NDVI	( $R_{nir} - R_{red}$ ) / (R...	
<input type="checkbox"/>	Simple Ratio	SR	( $R_{nir}$ ) / ( $R_{red}$ )

**Fit Settings**

ARTMO

Select	Funtion fitting	Equation
<input type="checkbox"/>	linear	$f(x) = m * x + b$
<input type="checkbox"/>	exponential	$f(x) = a + \exp(b * x)$
<input type="checkbox"/>	logarithmic	$f(x) = b + m * \log(x)$
<input type="checkbox"/>	power	$f(x) = b * (x^m)$
<input type="checkbox"/>	polynomial2	$f(x) = (a2 * (x^2)) + (a1 * x) + a0$

Outliers: Without analysis

**Noise settings**

Parameter Gaussian Noise [0-100%]   Range

Spectral Gaussian Noise [0-100%]   Range

**RTM data**

Train [0-100%]   Range

Only train  Only test

**USER data**

Train [0-100%]   Range

Only train  Only test

**Finished**

If active, configure per land cover class.

Select an Index group

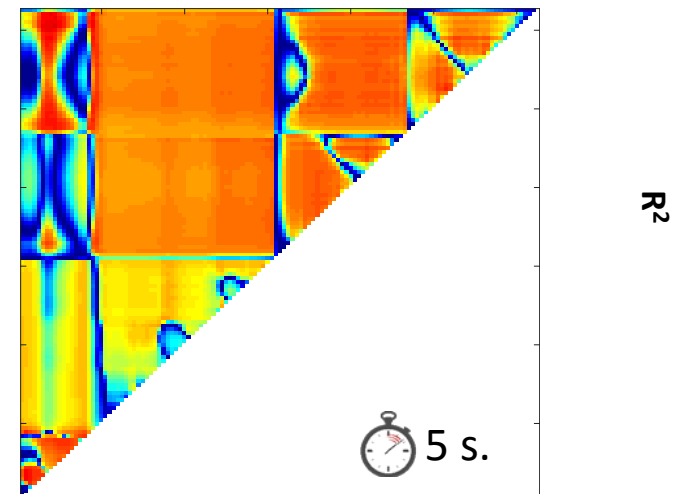
Select one or multiple indices

Select one or multiple curve fittings

Options to add noise

Option to mix RTM with field observations

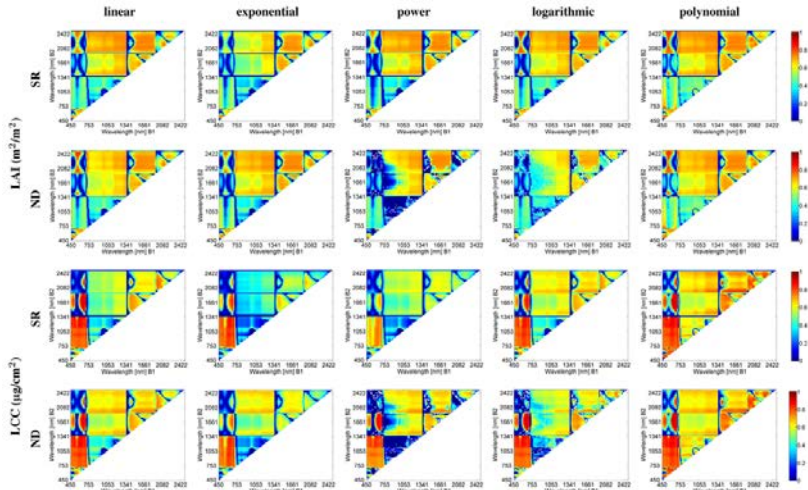
## SPARC – HyMap - LAI



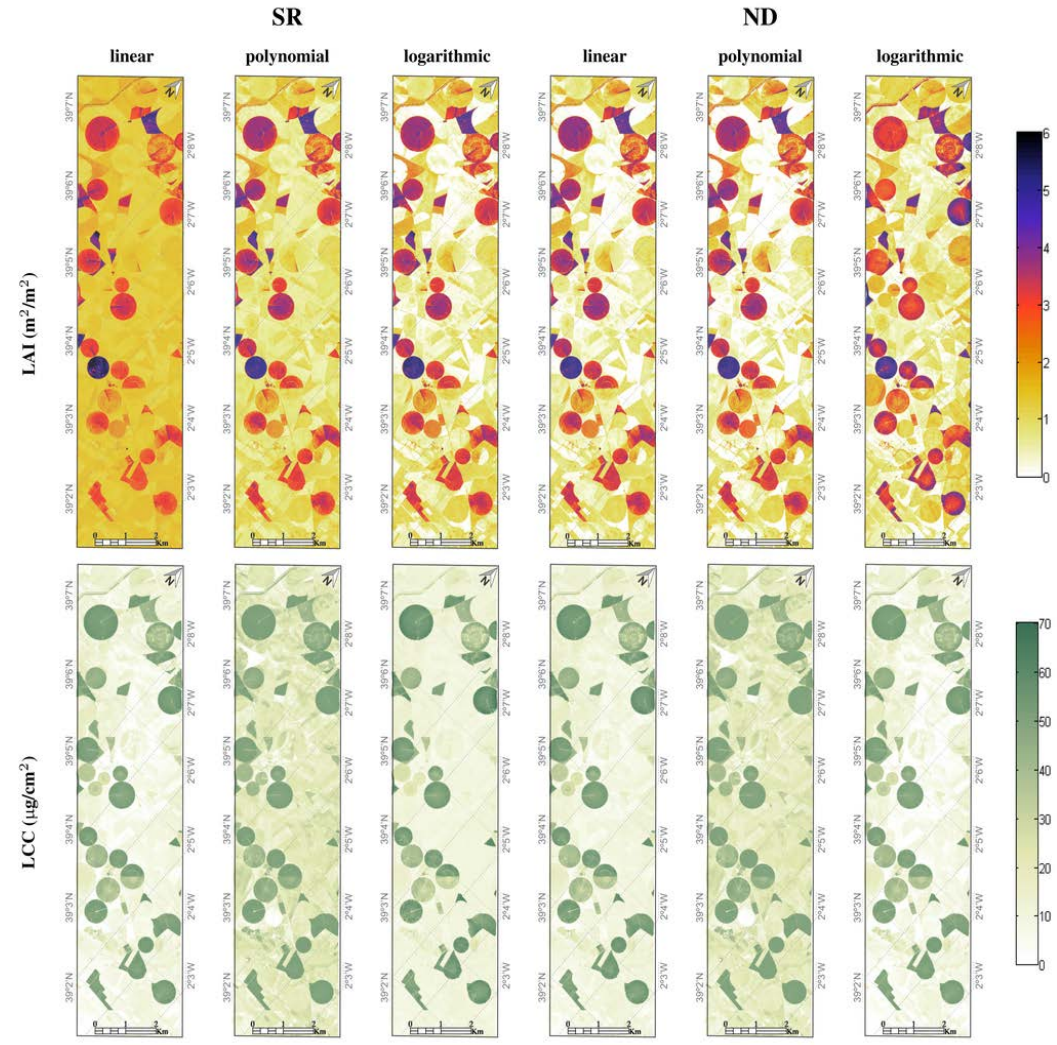
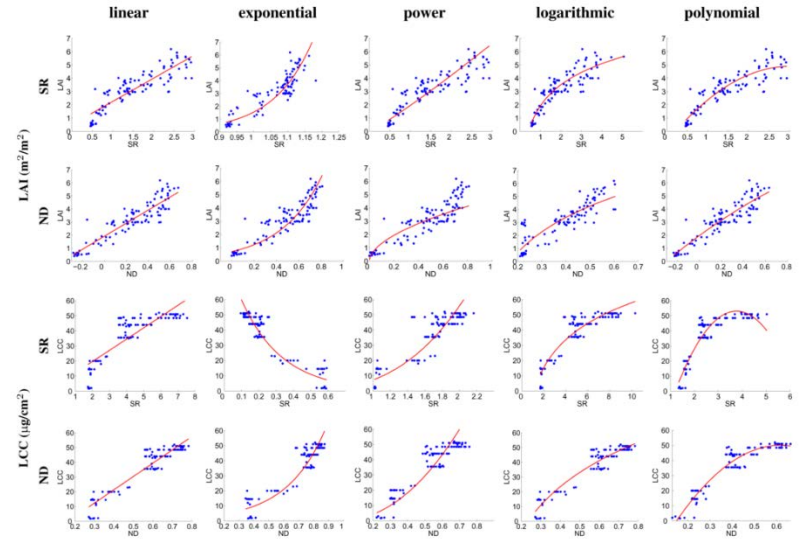
*Best-performing index can be applied to an image.*

# SPARC dataset (Barrax Spain); HyMap data

SR and ND for different fitting functions

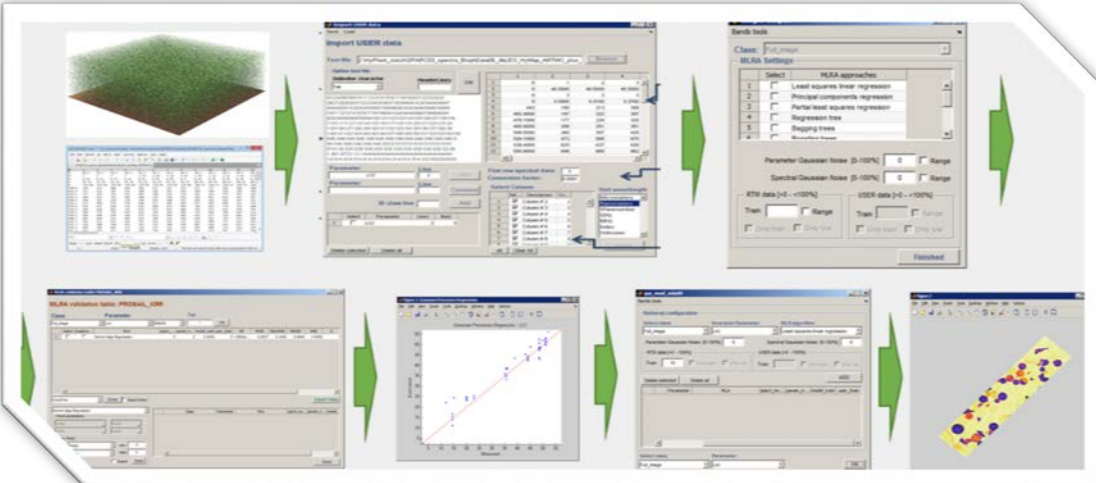
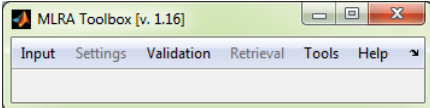


Best performing model.



- Which VI method is most correct?
- Why restricting to a few bands only?

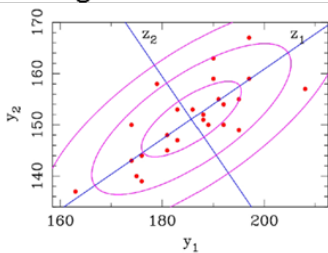
# Machine learning regression algorithm toolbox



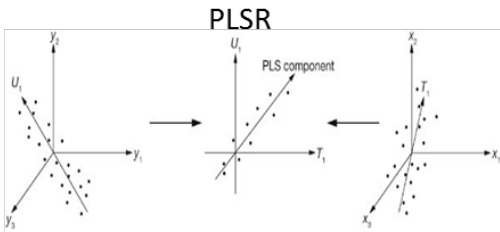
- Properties:**
- About 15 MLRAs implemented
  - Single-output & multi-output
  - Noise & Cross-validation options
  - Dimensionality reduction options
  - Results stored in MySQL
  - GPR properties: band relevance & uncertainties
  - Can process both images or individual spectra.
  - Active learning, GPR-BAT, dim. reduction

*Simpler to execute than SI: no band selection needed.*

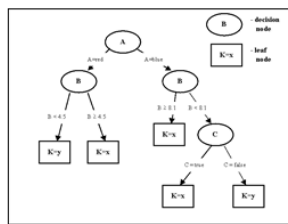
Principal component regression – PCR



Partial least squares regression



Decision Trees – DT



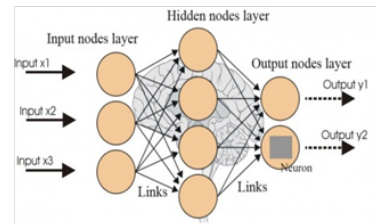
Non-parametric models:

- SimpleR [Camps-Valls et al., 2013]
- <http://www.uv.es/gcamps/code/simpleR.html>

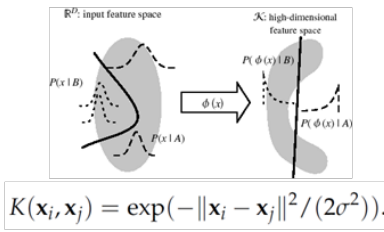
Also:

- Bagging trees (BAGTREE)
- Boosting trees (BOOST)
- Neural networks (NN)
- Extreme Learning Machines (ELM)
- Support Vector Regression (SVR)
- Relevance Vector Machine (RVM)
- Variational Heteroscedastic Gaussian Process Regression (VHGPR)

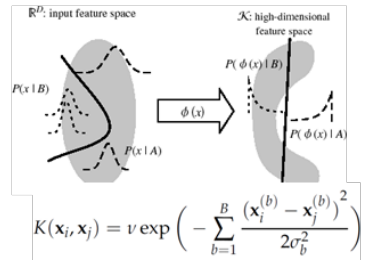
Neural networks  
NN



Kernel ridge regression  
KRR



Gaussian processes regression  
GPR



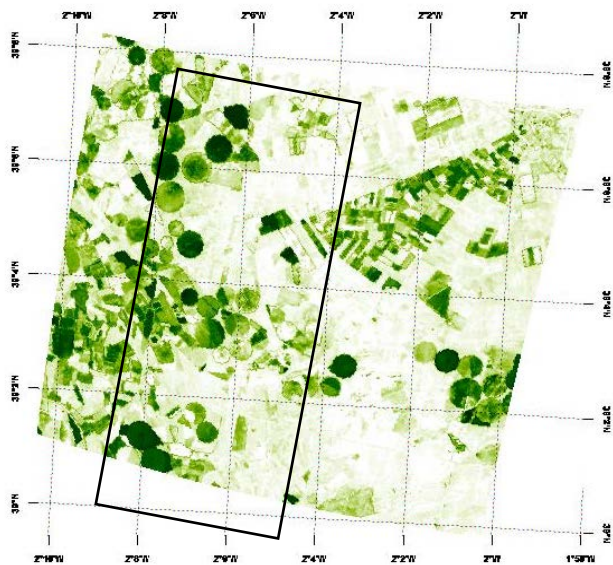
GPR in Bayesian framework also provides:

- Band relevance
- Uncertainty estimates



# GPR maps

CHRIS



LCC [ $\mu\text{g}/\text{cm}^2$ ]



St Dev

LCC [ $\mu\text{g}/\text{cm}^2$ ]

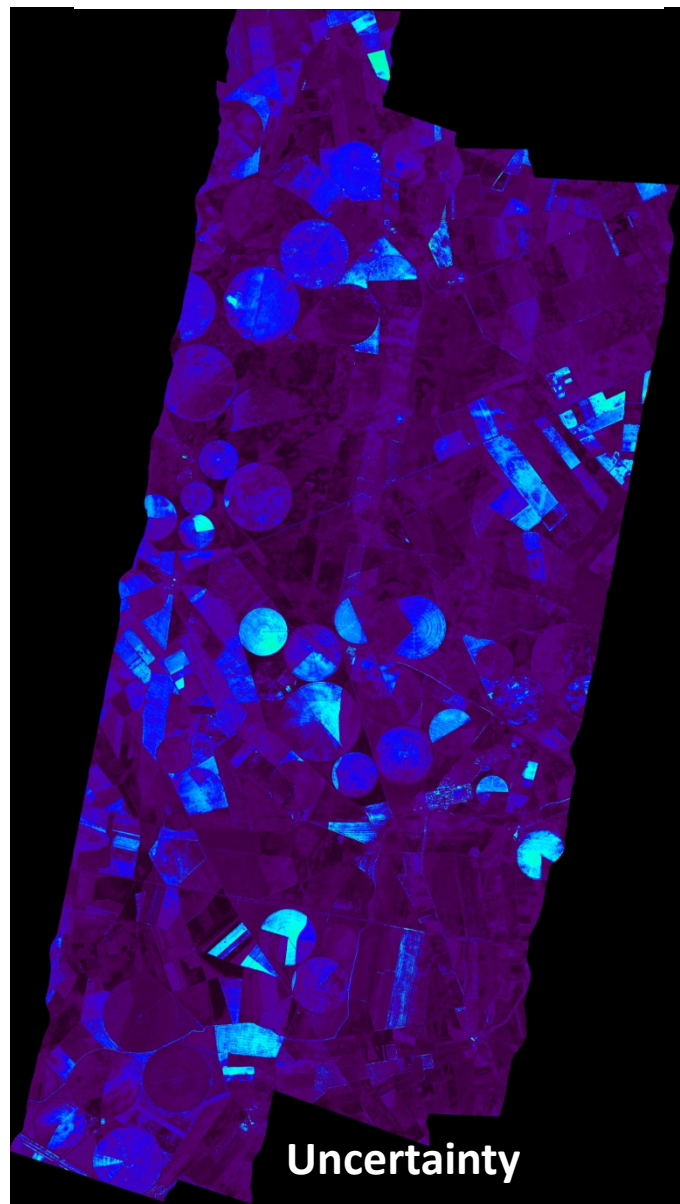
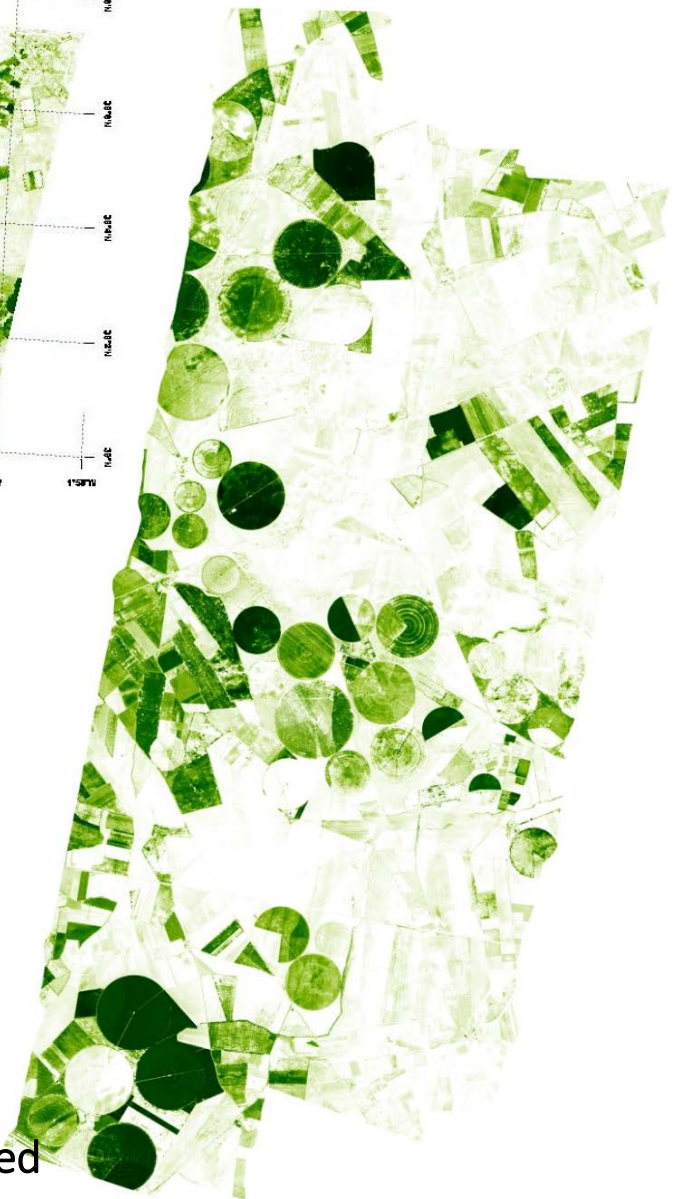


CASI1500

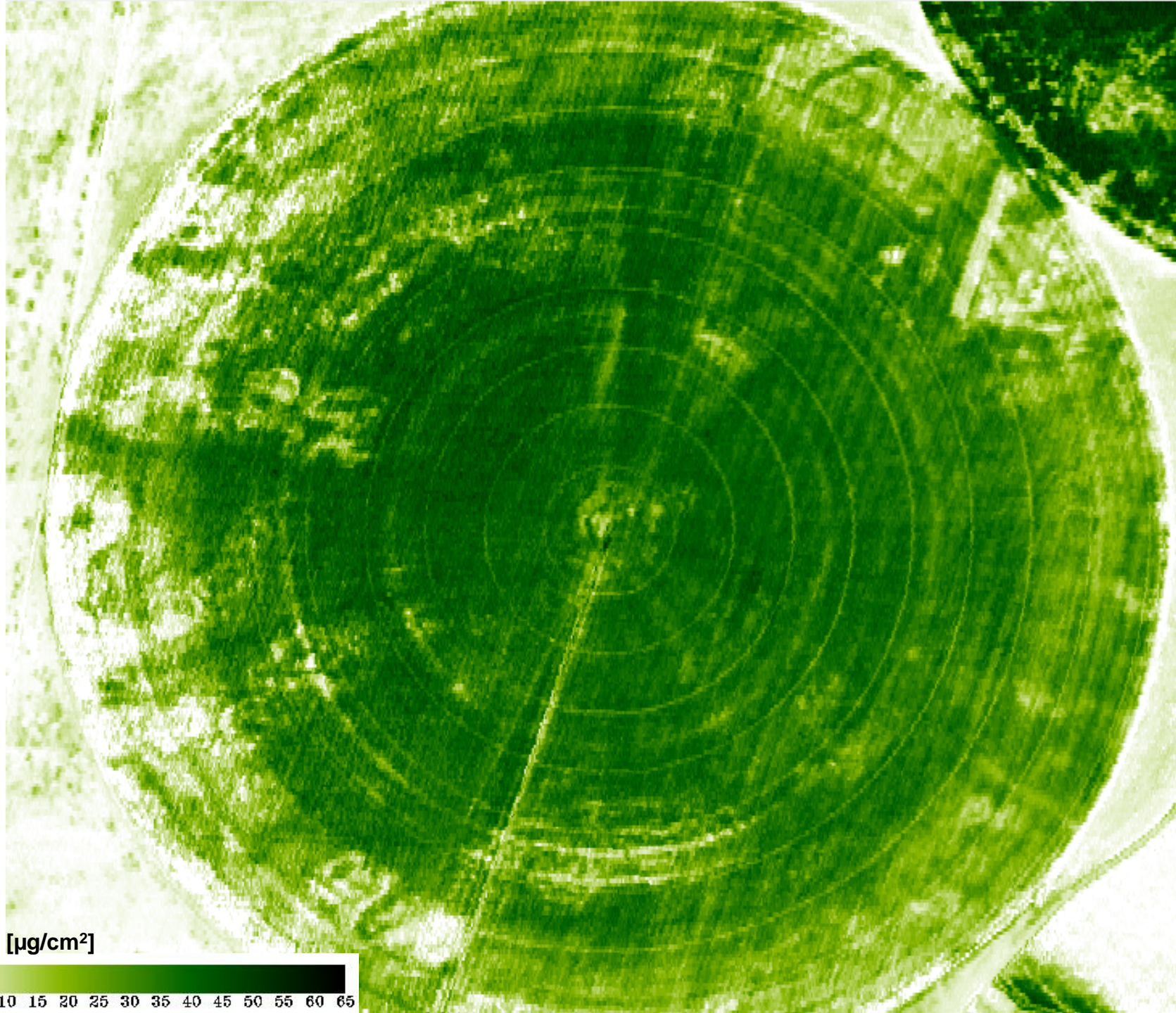
- pixel size: 1.4m

- 288 bands

Same GP model was applied



Uncertainty

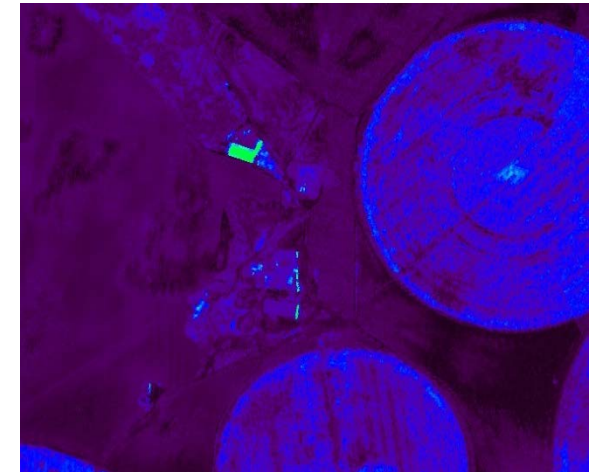
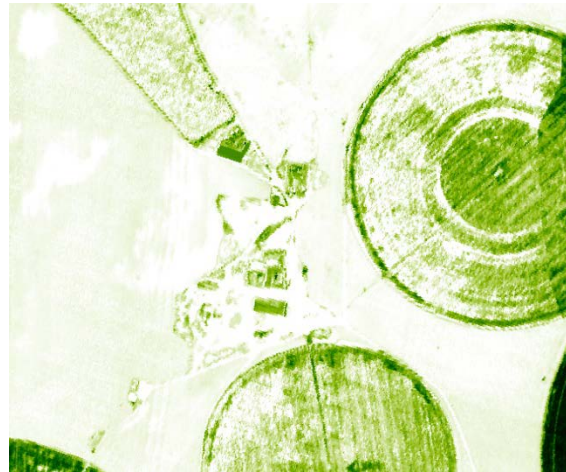
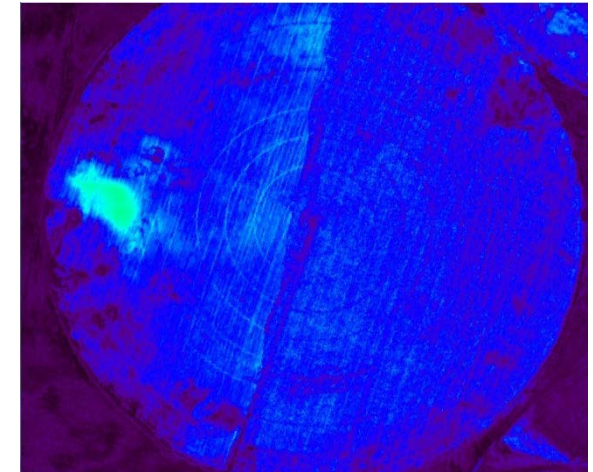
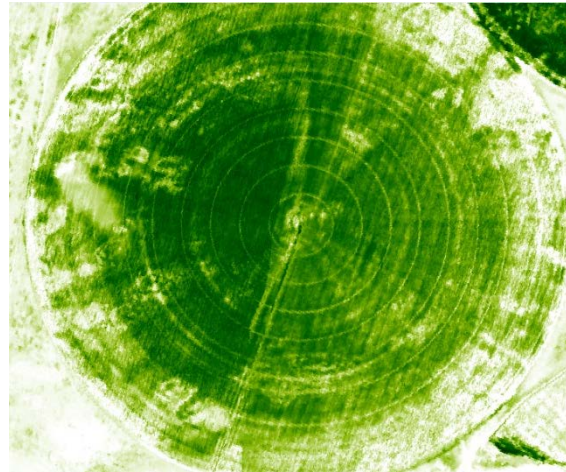
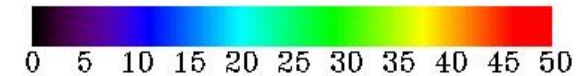
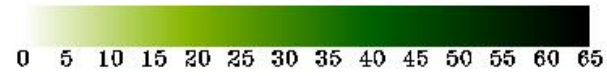


LCC [ $\mu\text{g}/\text{cm}^2$ ]



St Dev  
LCC [ $\mu\text{g}/\text{cm}^2$ ]LCC [ $\mu\text{g}/\text{cm}^2$ ]

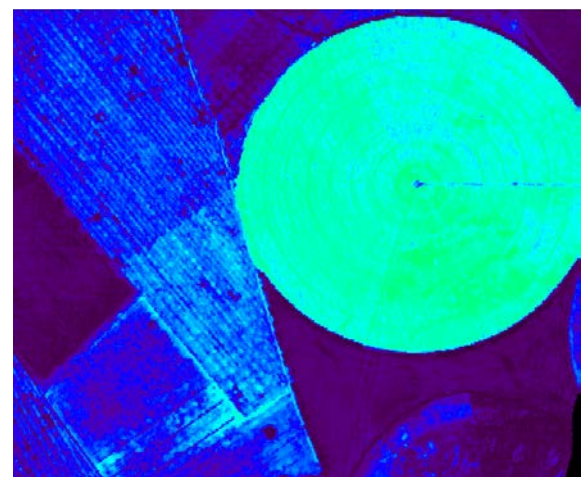
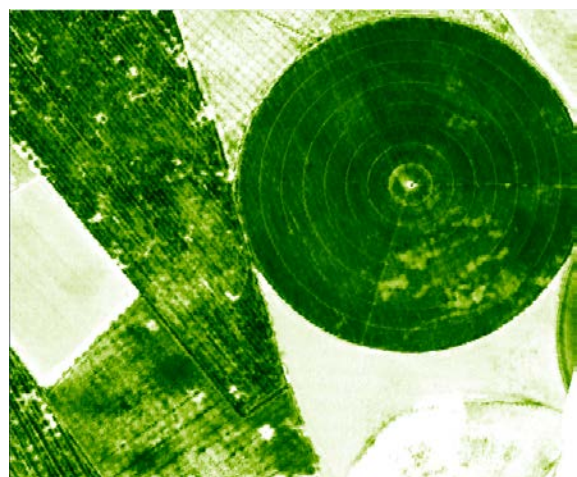
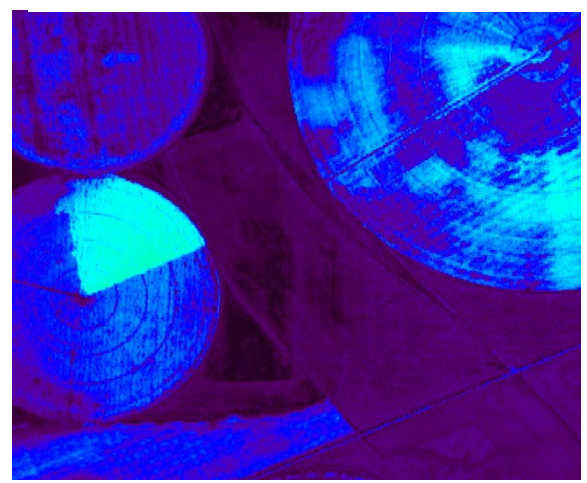
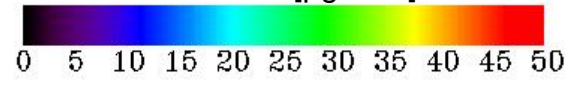
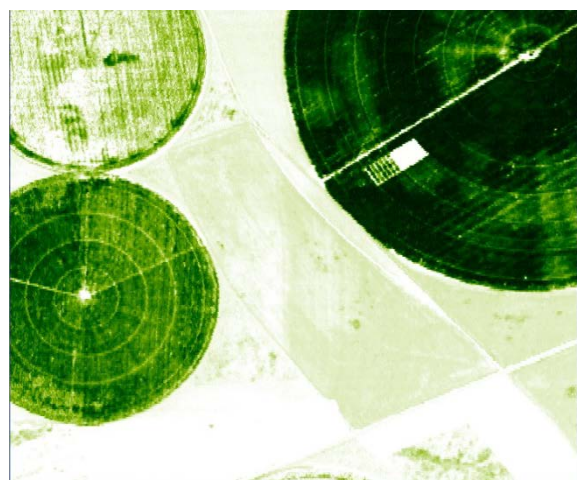
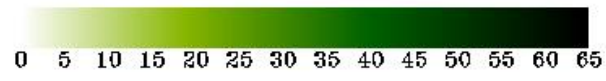
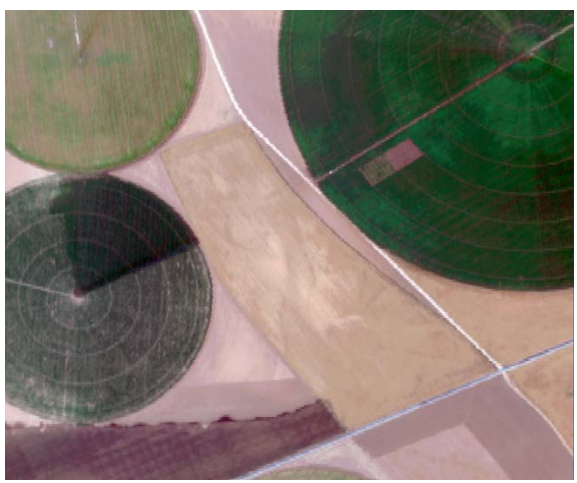
RGB CASI



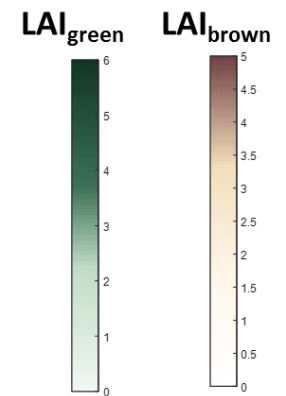
- **Uncertainty maps** provide **additional info** which may be hidden on the images.
- **Implausible estimations** are detected.

LCC [ $\mu\text{g}/\text{cm}^2$ ]

RGB CASI



- In turn, **despite low uncertainties also good estimations**. No impact on recently irrigated areas (other methods have difficulties with wet soils).
- For operational applications, of interest to flag/mask regions with high uncertainties.



## GPR to S2

GPR Retrievals with uncertainties <40% masked out (removes directly non-vegetated surfaces).

# The challenge of machine learning applied to imaging spectroscopy

- *Machine learning methods are adaptive and can be very powerful. However that goes a computational cost. This can be problematic when large datasets are involved, either in the sampling or in the spectral domain (e.g. for hybrid methods).*
- *Moreover, when many bands are involved: multicollinearity leads to statistical problems (suboptimal performance).*

## *Solutions to deal with large datasets:*

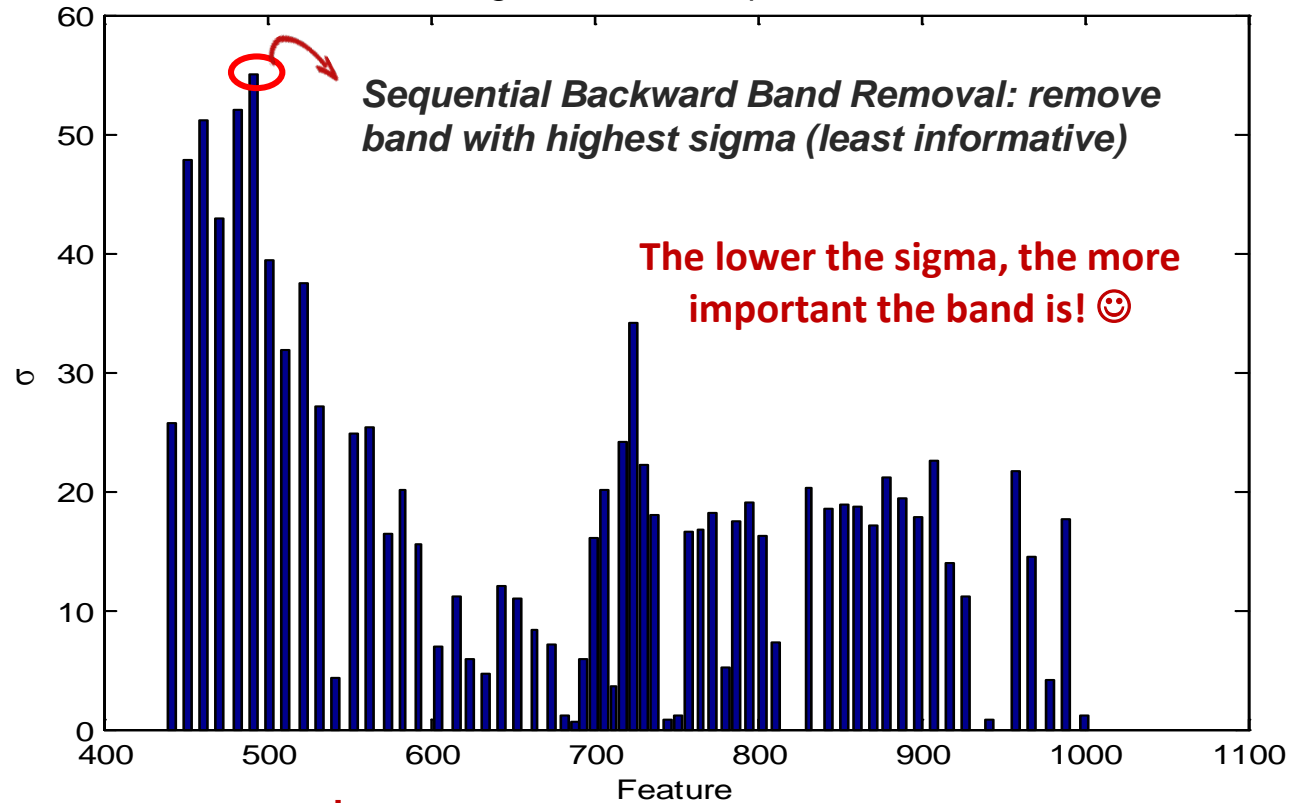
### **1.Reducing spectral data:**

- I. band selection (GPR-BAT),
- II. dimensionality reduction

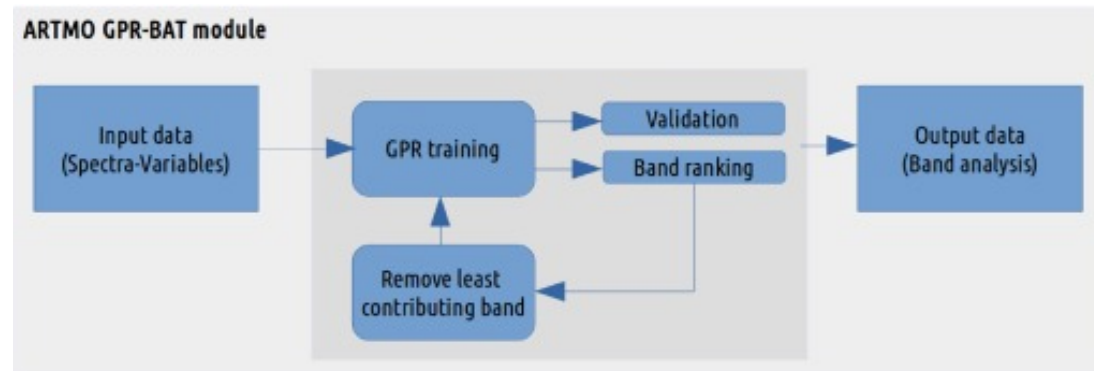
### **2.Samples reducing : Active learning**

# I) Band selection: GPR-BAT

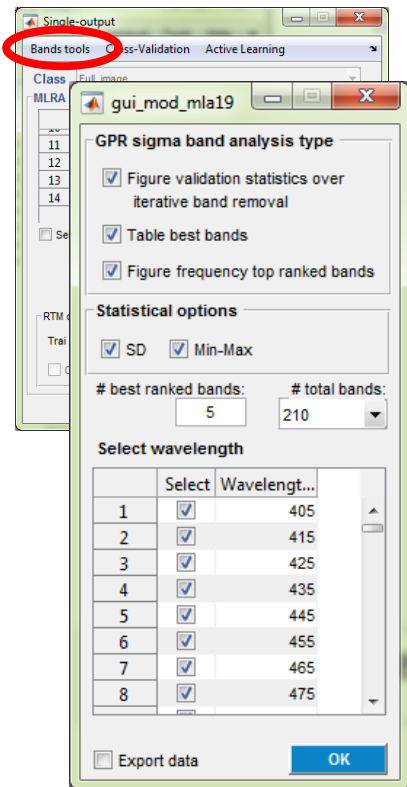
Gaussian processes regression – Band analysis Tool (GPR-BAT).



automated



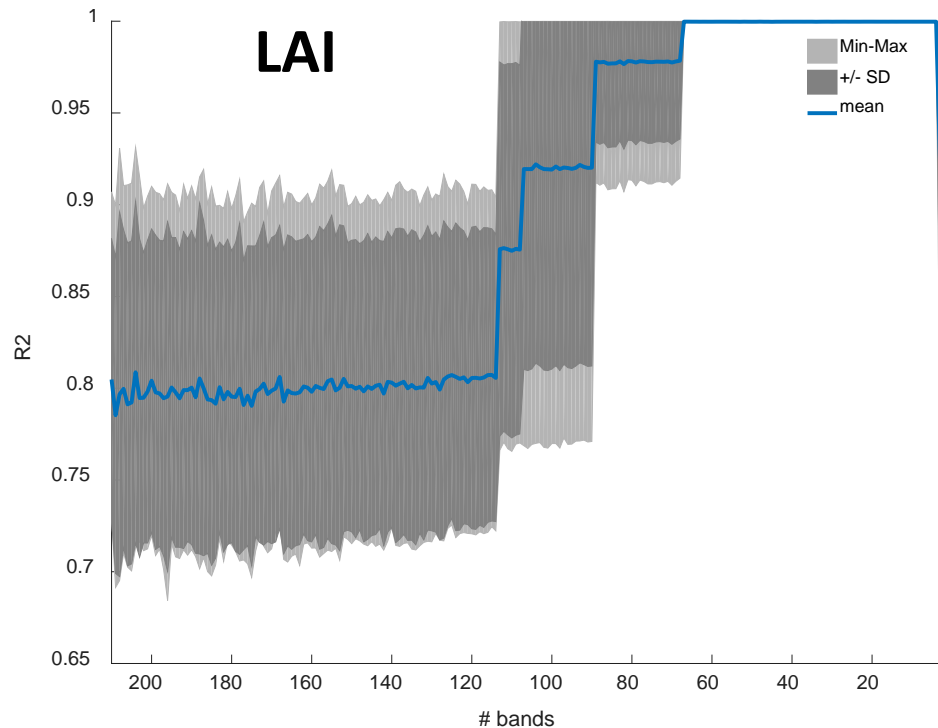
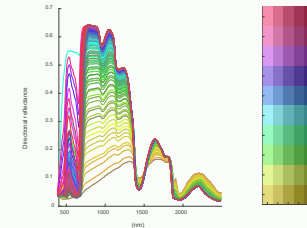
*Best-performing method can be applied to an image.*



# GPR-BAT example with simulated data (PROSAIL)

## Experimental setup:

- PROSAIL: LHS 100# @ 10 nm, 220b; Cab, LAI
- 4k cross-var sampling

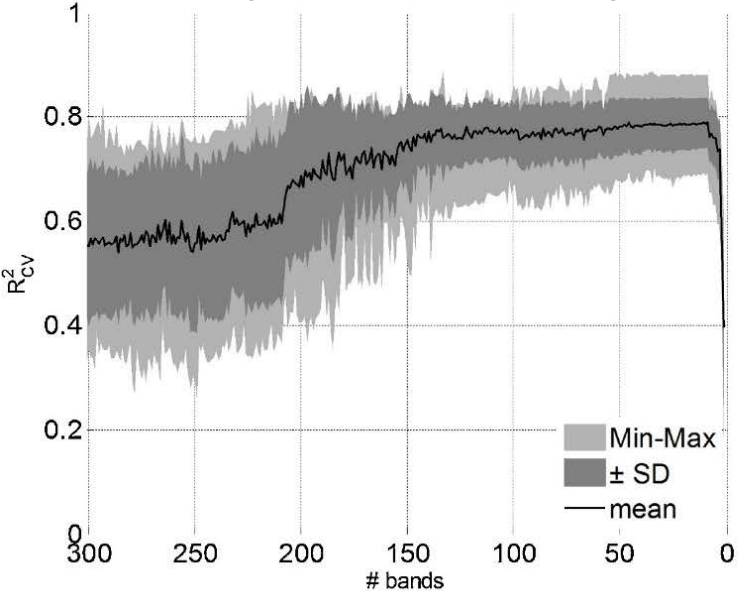


# band	R2	wavelengths
5	<b>0.9997</b>	815, 1145, 1205, 122, 1245
4	<b>0.9997</b>	815, 1145, 1205, 1245
3	0.9213	815, 1145, 1205
2	0.8104	815, 1145
1	0.8104	815

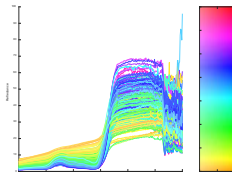
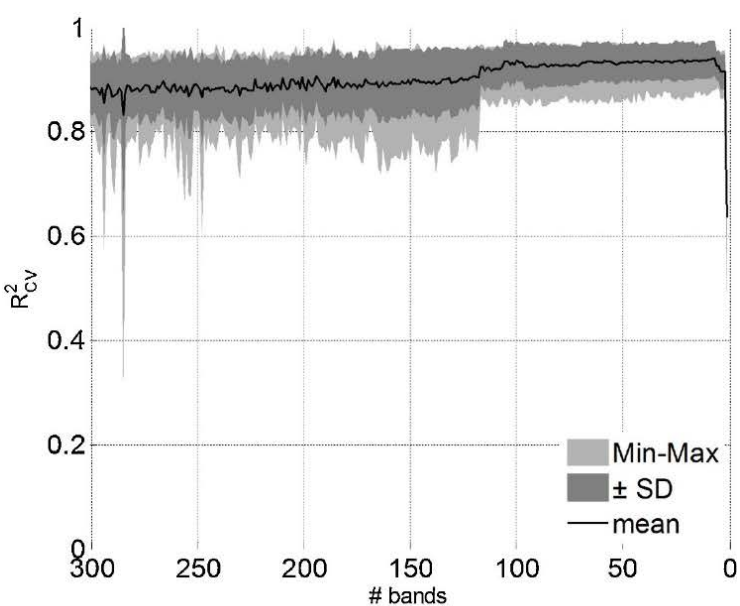
**Best performances achieved between 70 and 4 bands  
(using all bands or <3 bands not recommended)**



LCC (best with 9 bands)

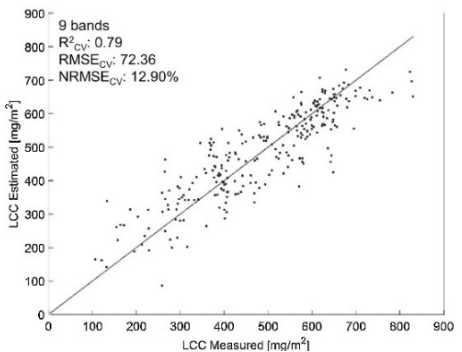


gLAI (best with 7 bands)



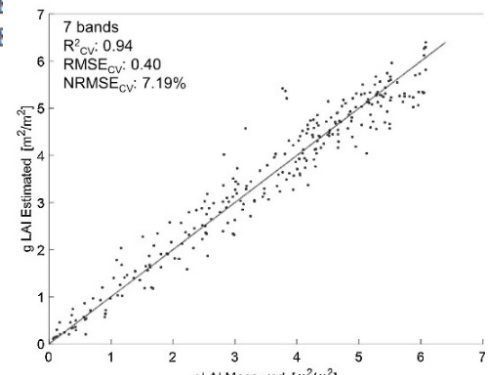
All bands

- ...
- 482, 500, 564, 566, 710, 712, 714, 878, 966, 980
- 482, 500, 564, 710, 712, 714, 878, 966, 980**
- 482, 500, 564, 710, 712, 714, 878, 966
- 482, 500, 564, 710, 714, 878, 966
- 482, 500, 710, 714, 878, 966
- 500, 710, 714, 878, 966
- 500, 710, 714, 878
- 500, 710, 878
- 500, 710
- 710

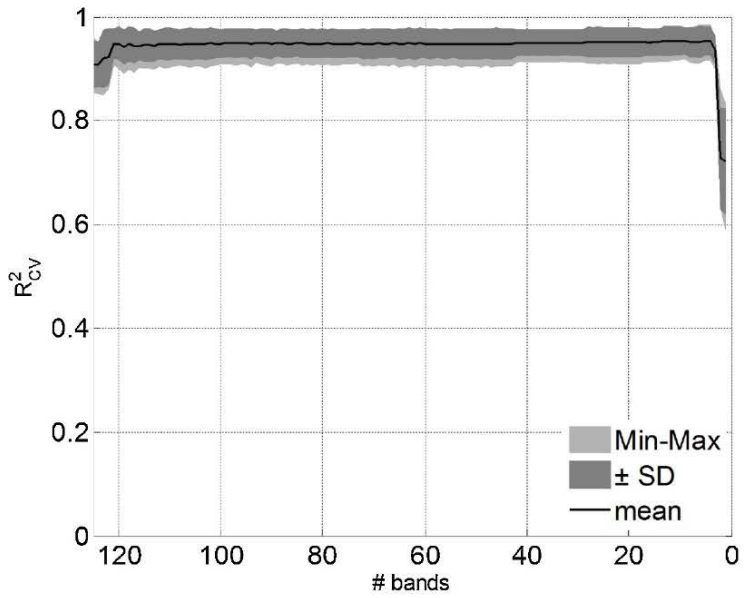


All bands

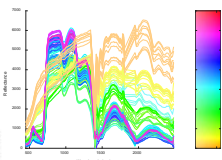
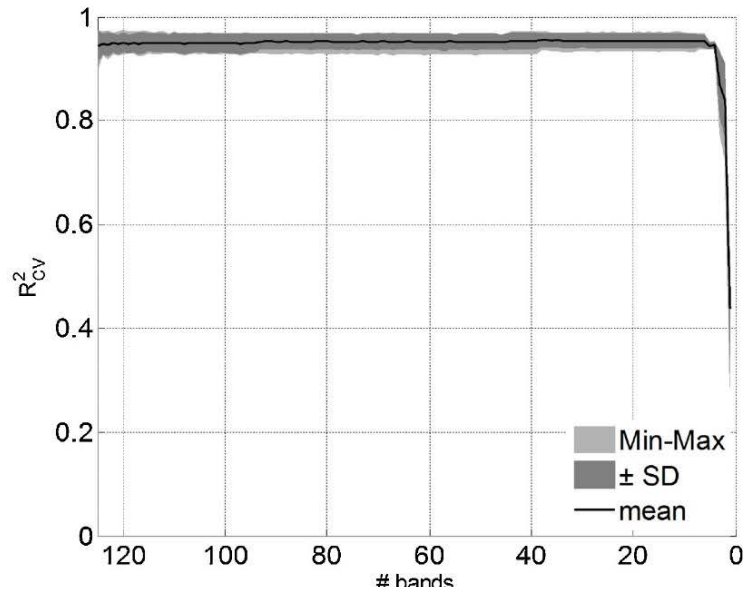
- ...
- 406, 746, 770, 790, 792, 794, 798, 808, 858, 878
- 406, 746, 790, 792, 794, 798, 808, 858, 878
- 406, 746, 790, 792, 794, 798, 858, 878
- 406, 746, 792, 794, 798, 858, 878**
- 746, 792, 794, 798, 858
- 746, 792, 794, 798, 878
- 746, 792, 794, 798
- 746, 792, 794
- 746, 792
- 792



LAI (best with 4 bands)

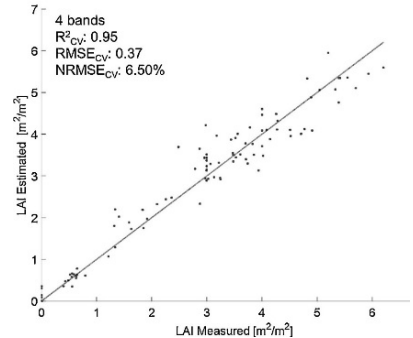


CWC (best with 6 bands)



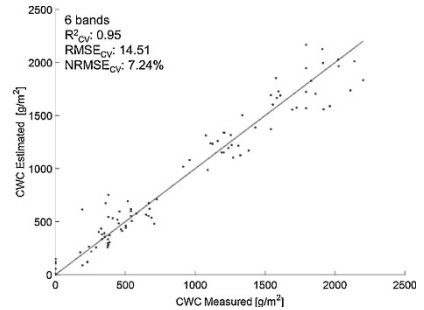
All bands

- ⋮
- 462, 478, 708, 723, 1215, 1243, 1272, 1327, 1635, 2483
- 462, 478, 708, 723, 1215, 1243, 1272, 1327, 2483
- 462, 478, 708, 723, 1215, 1243, 1272, 1327
- 462, 478, 708, 723, 1215, 1272, 1327
- 462, 478, 708, 723, 1215, 1327
- 462, 478, 708, 723, 1327
- 462, 708, 723, 1327**
- 462, 708, 1327
- 462, 1327
- 462

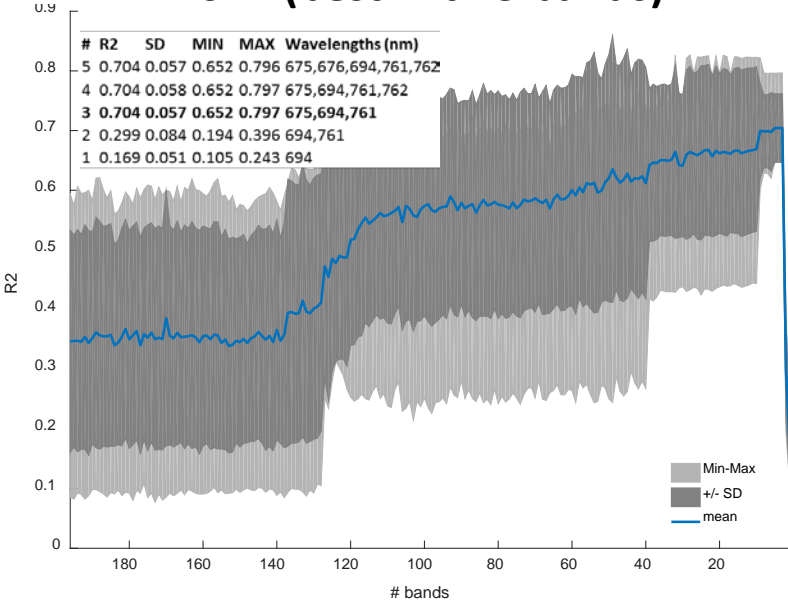


All bands

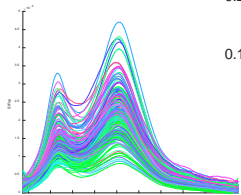
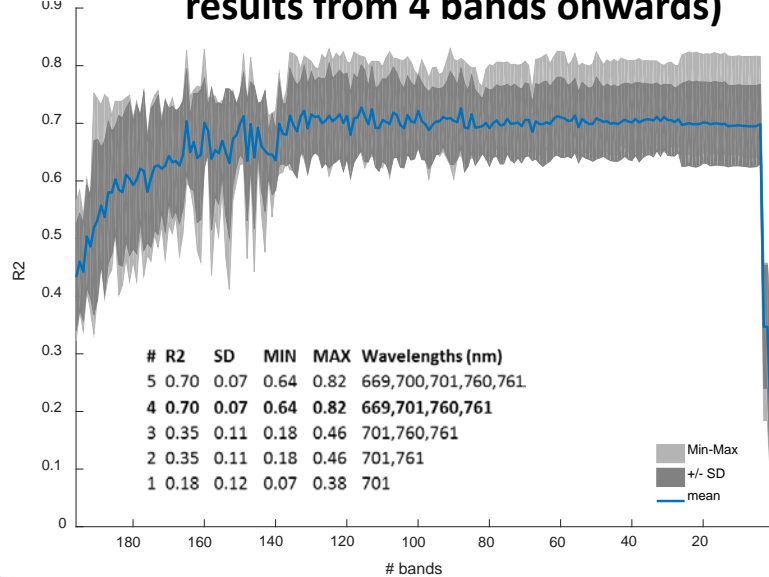
- ⋮
- 462, 723, 1128, 1157, 1272, 1286, 1299, 1327, 1419, 2483
- 723, 1128, 1157, 1272, 1286, 1299, 1327, 1419, 2483
- 723, 1128, 1157, 1272, 1286, 1327, 1419, 2483
- 723, 1128, 1157, 1272, 1286, 1327, 1419
- 723, 1157, 1272, 1286, 1327, 1419**
- 723, 1157, 1272, 1286, 1327
- 723, 1157, 1272, 1286
- 1157, 1272, 1286
- 1157, 1286
- 1286



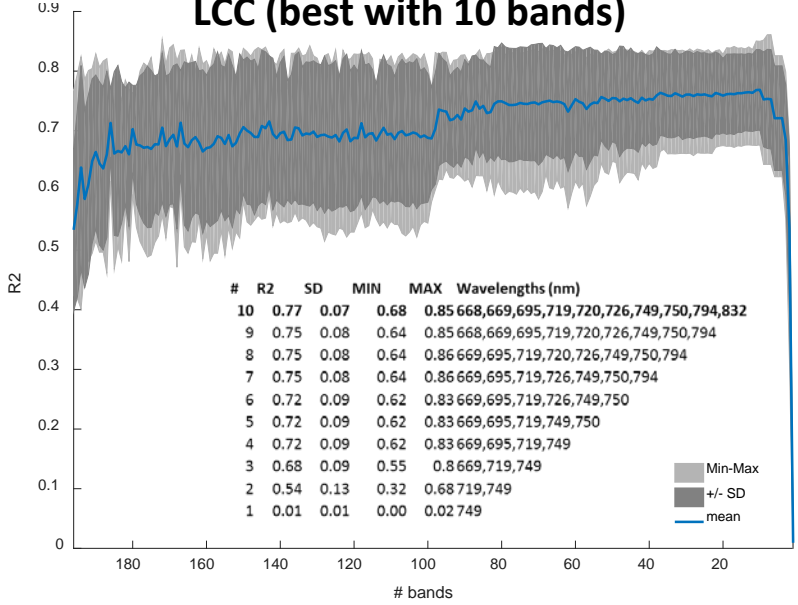
### SLA (best with 3 bands)



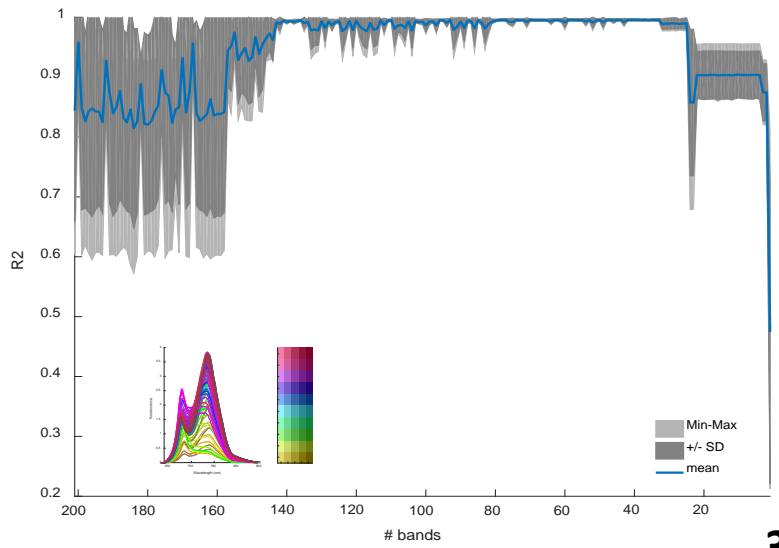
### LWC (best with 116 bands, stable results from 4 bands onwards)



### LCC (best with 10 bands)



### SCOPE: LAI (best at 44 bands)



# II) Dimensionality reduction: SIMFEAT

**Single-output**  
 Bands tools | Cross-Validation | Active Learning

Class: Full\_image

**MLRA Settings**

Select	MLRA approaches
<input type="checkbox"/>	Extreme Learning Machine
<input checked="" type="checkbox"/>	Kernel ridge Regression
<input type="checkbox"/>	Gaussian Processes Regression
<input type="checkbox"/>	VH. Gaussian Processes Regression

Parameter Gaussian Noise [0-100%]: 0  Range  
 Spectral Gaussian Noise [0-100%]: 0  Range

RTM data [>0 - <100%]: Trai  Range  
 USER data [>0 - <100%]: Trai 20  Range

**Simple Feature Extraction Toolbox [SIMFEAT]**

File Cluster

**Feature Extraction Algorithms**

Select	Band reduction methods	Kernel type
<input type="checkbox"/>	Principal component analysis (PCA)	Empty
<input type="checkbox"/>	Partial least squares (PLS)	Empty
<input type="checkbox"/>	Primal Partial least squares (PPLS)	Empty
<input type="checkbox"/>	Ortho-normalized PLS (OPLS)	Empty
<input type="checkbox"/>	Canonical correlation analysis (CCA)	Empty
<input type="checkbox"/>	Minimum Noise Fraction (MNF)	Empty
<input type="checkbox"/>	Principal Component of KECA method (KECA)	rbf
<input type="checkbox"/>	Kernel Principal Component Analysis (KMNf)	rbf
<input type="checkbox"/>	Kernel Principal Component Analysis (KPCA)	rbf
<input type="checkbox"/>	Kernel dual partial least squares (KDPLS)	rbf
<input type="checkbox"/>	Kernel partial least squares (KPLS)	rbf
<input type="checkbox"/>	Kernel Orthonormalized Partial Least Squares (KOP...)	rbf
<input type="checkbox"/>	Kernel Canonical Correlation Analysis (KCCA)	rbf

# Feature: 5 **OK**

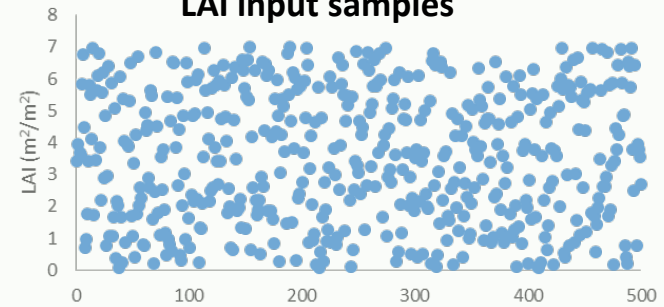
*13 dimensionality reduction methods implemented.*

## Experimental setup:

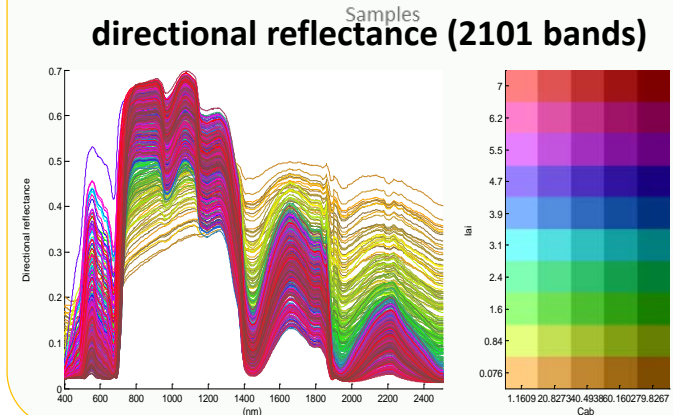
**PROSAIL: 500 random samples**

Variable	Min	Max
N	1.3	2.5
Cab	1	80
Cw	0.002	0.05
Cm	0.002	0.05
LAD	0	90
LAI	0.01	7

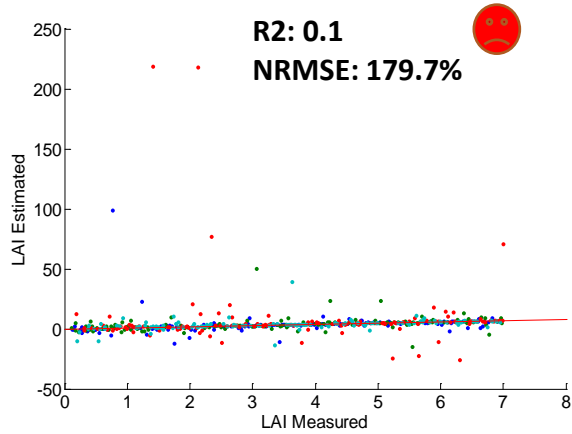
**LAI input samples**



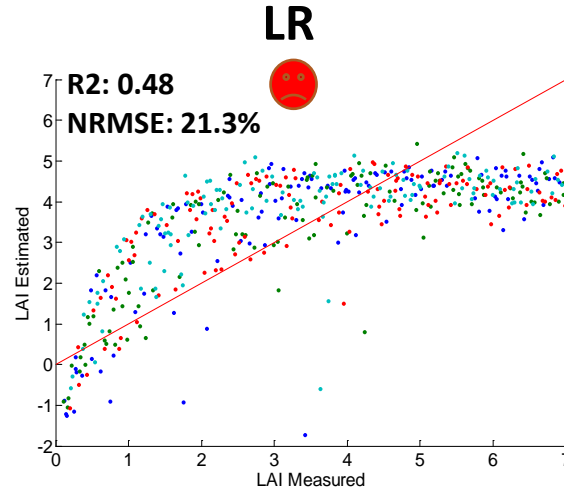
**directional reflectance (2101 bands)**



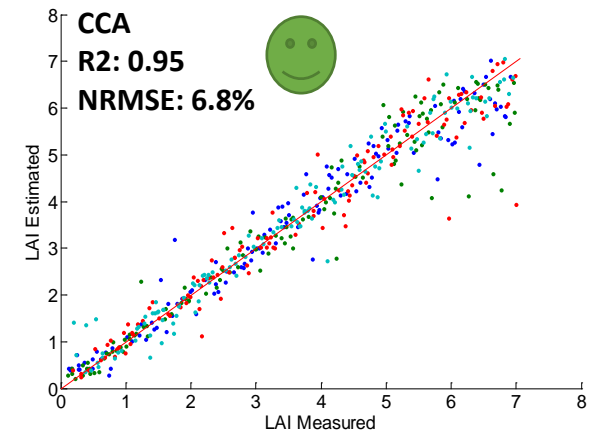
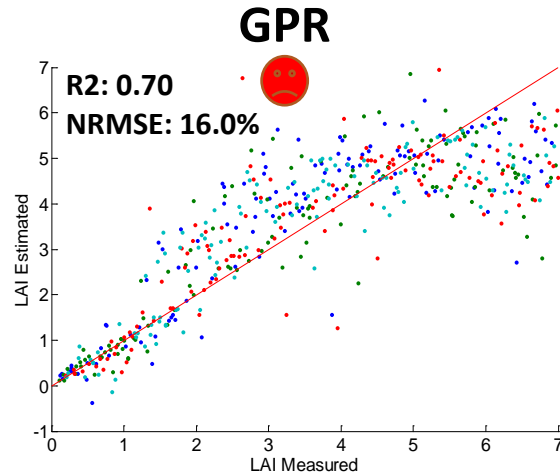
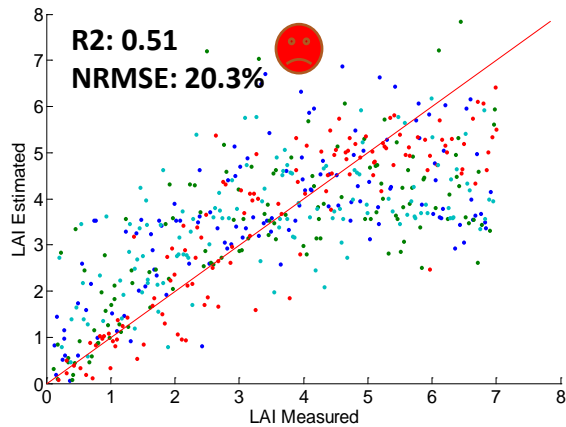
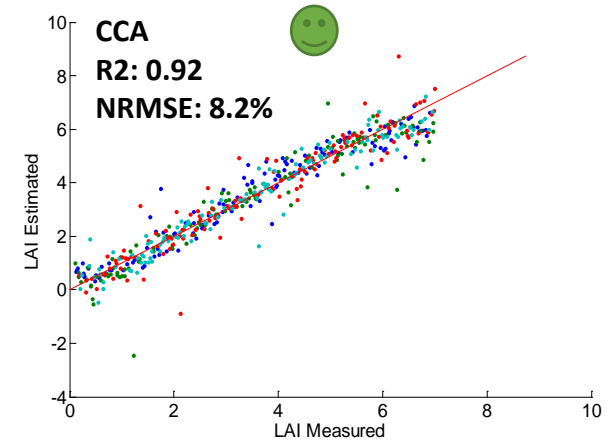
No DR (2101#)



PCA (5#)

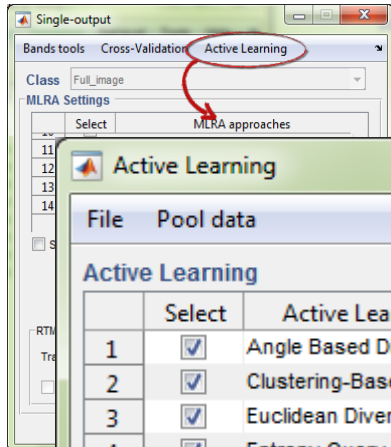


Best DR method (5#)

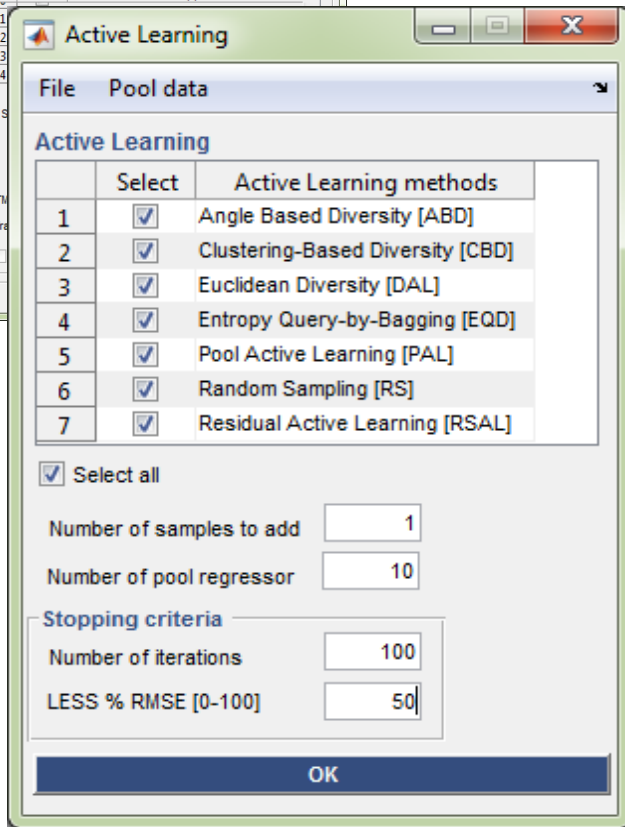


By combining advanced DR methods with (advanced) regression methods, hyperspectral data can be exploited to the fullest. Or, full spectral dataset into regression require (advanced) DR methods. 37/55

## 2) Sample reduction: Active learning (AL)



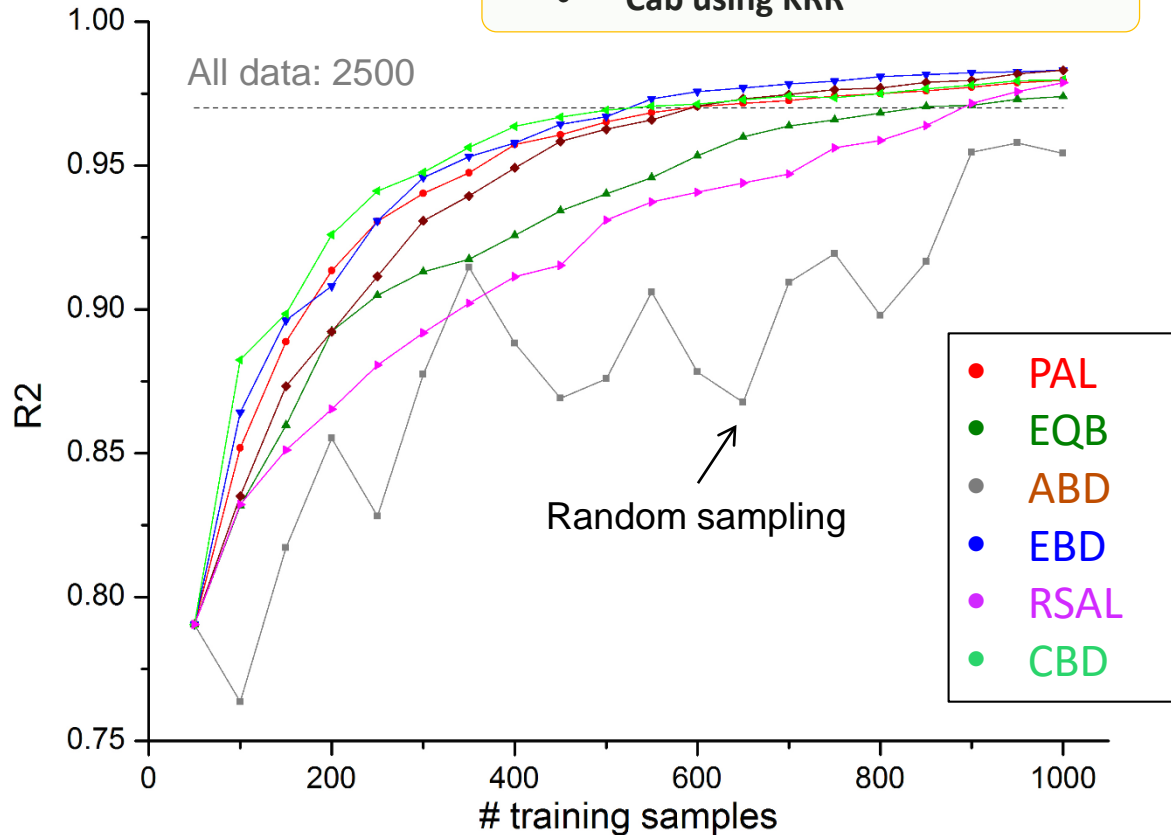
*6 AL methods implemented.*



### Experimental setup:

PROSAIL: 5000 samples

- 2500 training; 2500 validation
- Cab using KRR

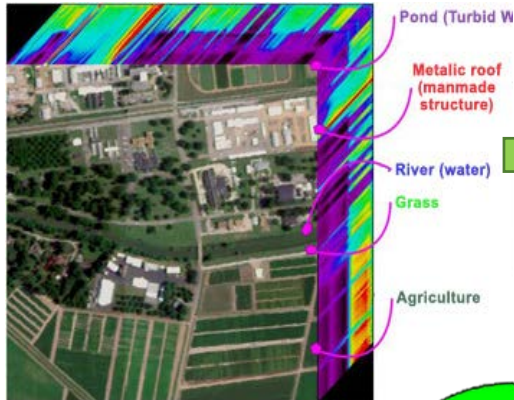


- Active learning (AL) searches for new samples from a data pool based on **uncertainty** (PAL, EQB, RSAL) and **diversity** (ABD, CBD, EBD).
- AL method search more efficiently for relevant samples than random sampling or when using all data.

*Best-performing method can be applied to an image.*

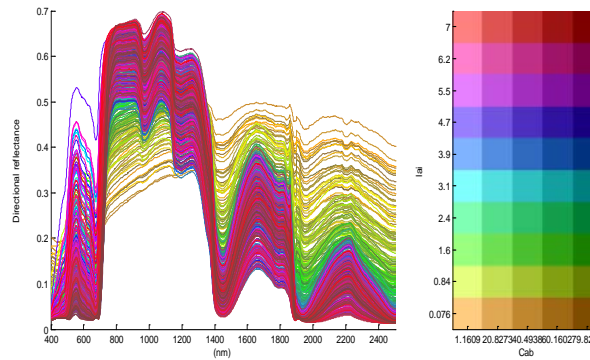
# Background LUT-based inversion

## RS imagery



Spectral block with 64 bands from 415 nm to 900 nm

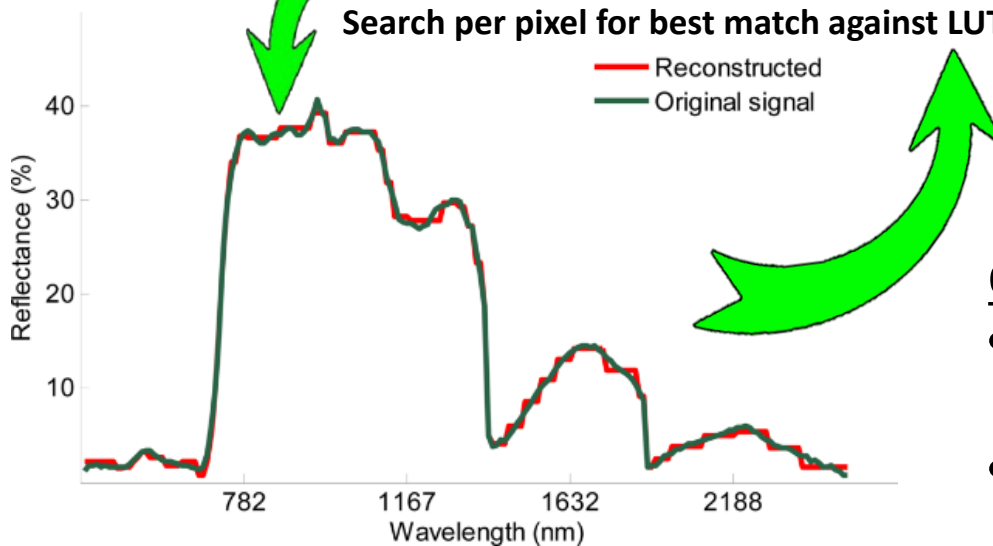
## PROSAIL LUT



Best match is obtained through a 'Cost function', or 'Minimum distance function'.

CostFunction	Definition	Minimum	Maximum
$C^{LS}$	$\sum(Y - X)^2$	0	$\infty$
$C^{NC}$	$\frac{\sum(X \cdot Y)}{\sqrt{\sum X^2} \sqrt{\sum Y^2}}$	-1	1
$C^W$	$\sum_k \frac{n_k}{N} \frac{\sqrt{\text{Var}(Y_k)}}{\mu(Y_k)}$	0	$\infty$
$C^{CR}$	$\frac{1}{\text{Var}(Y)} \sum_k \frac{n_k}{N} \text{Var}(Y_k)$	0	1

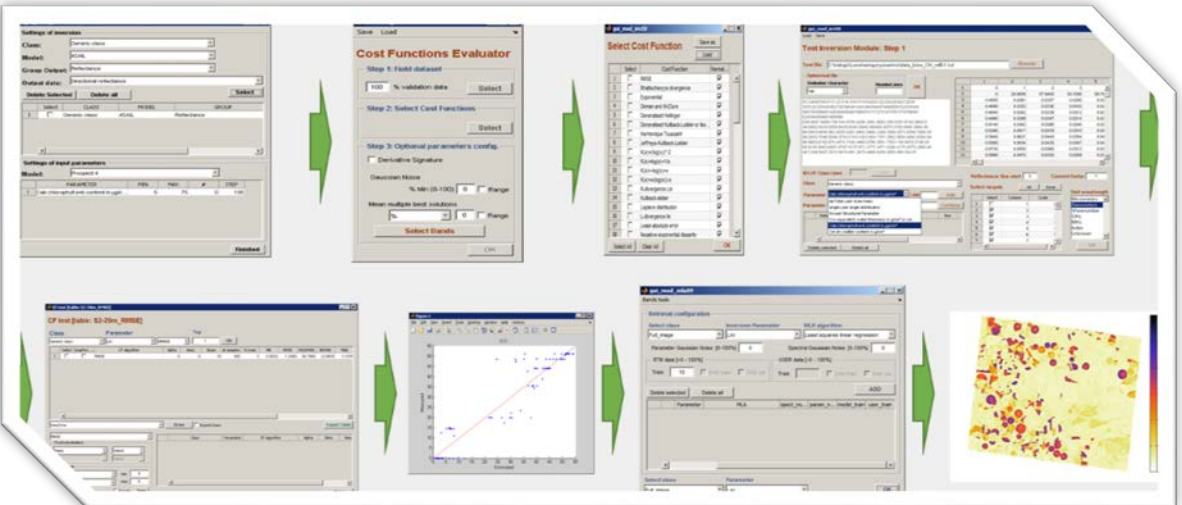
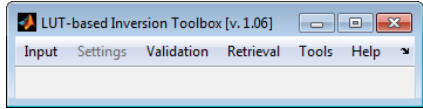
Search per pixel for best match against LUT



## Other important factors:

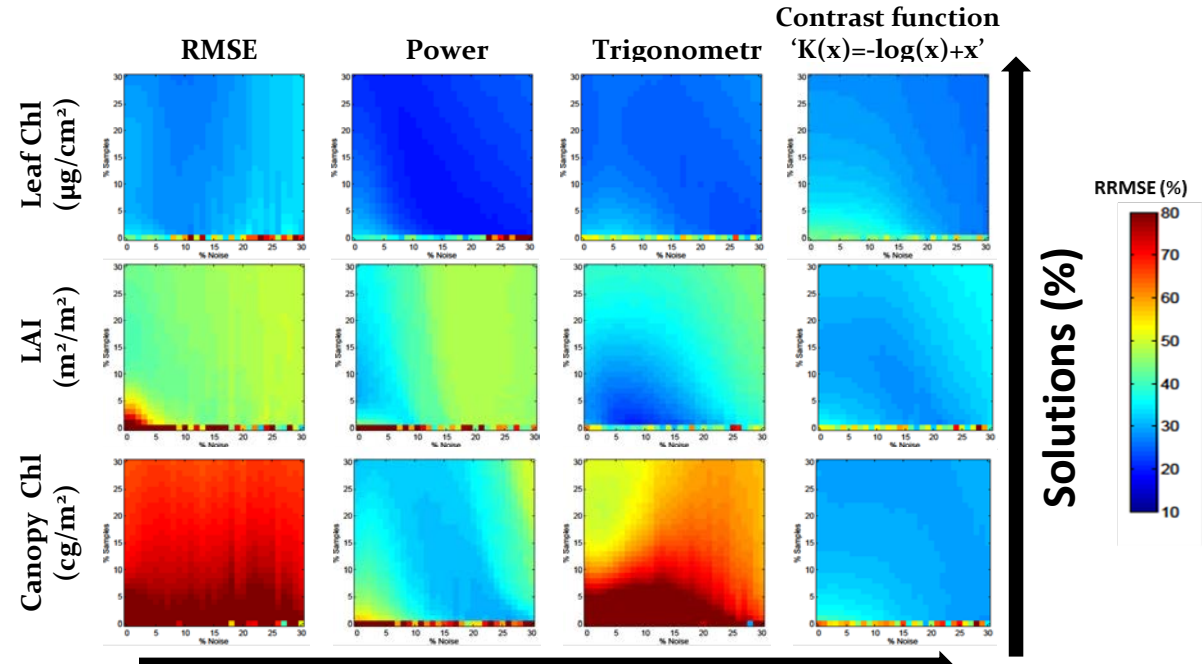
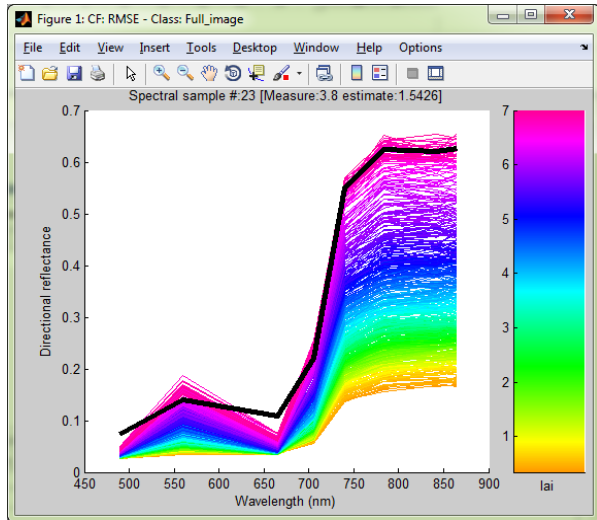
- Adding noise (to account for natural variability)
- Selecting mean/median of multiple solutions

# LUT-based inversion toolbox:



- Properties:**
- LUT ARTMO RTMs or external LUT
  - Over 60 different cost functions
  - Noise & multiple solutions
  - Results stored in MySQL
  - Top-performing inversion strategies are given.
  - Can apply inversion to both image or individual spectra.

## Matching a pixel against a part of the LUT.



Best-performing method can be applied to an image.

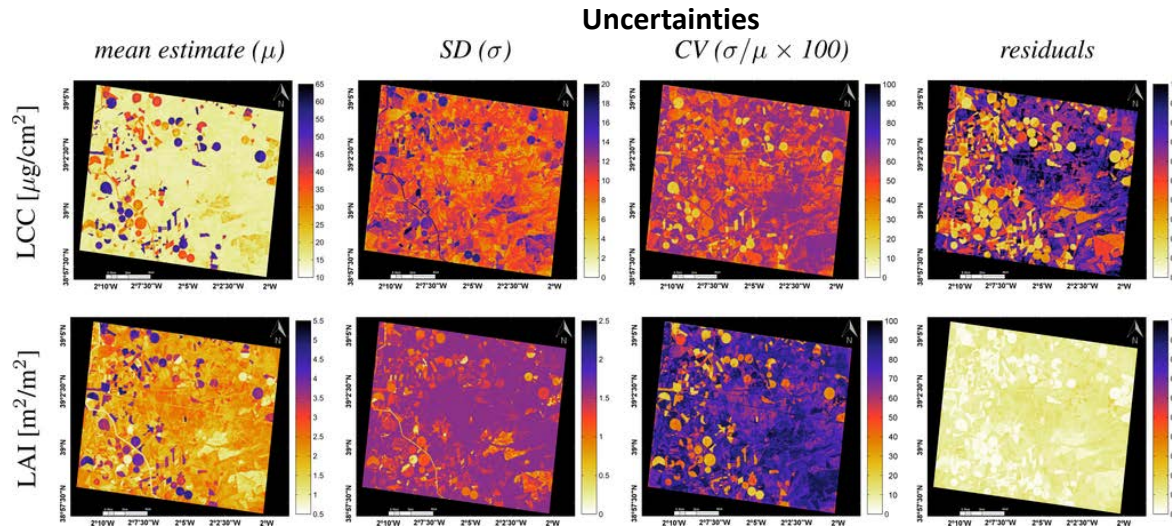
Noise (%)

40/55



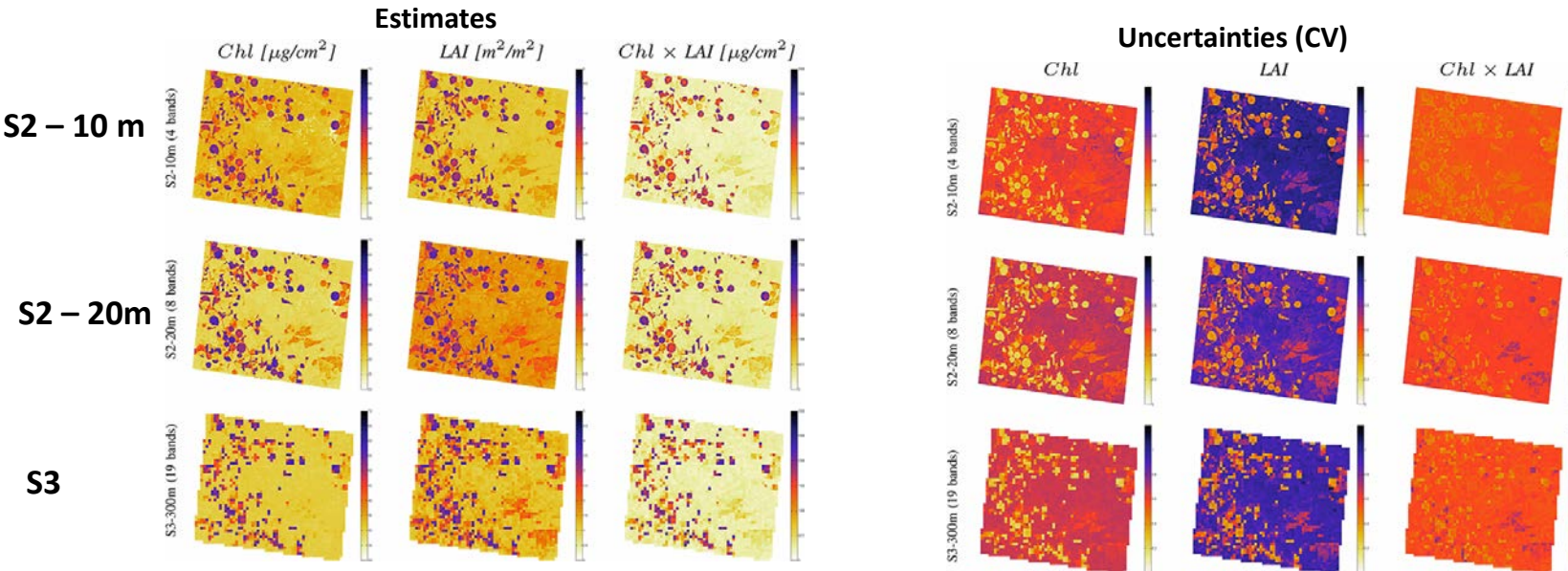
S2, 20m

Optimized cost function for each variable.



One optimized cost function for simultaneous retrieval of multiple variables.

Sentinel	S2-10m	S2-20m	S3-300m
Spatial resolution [m]	10	20	300
# bands	4	8 (4 + 4 at < 20 m)	19
Band position	B2, B3, B4 and B8	B2 to B8a	O2 to O20
Wavelengths [nm]	490-665 and 842	490-865	413-940



# SIMPLIFYING

- Global sensitivity analysis
- Emulation
- Retrieval



# Global sensitivity analysis

**Global sensitivity analysis**: explores the full input parameter space, i.e. all input parameters are changed together.

**Variance-based methods**: the output variance is decomposed to the sum of **contributions of each individual input parameter and the interactions** (coupling terms) between different parameters.

Based on the work of **Sobol'**, **variance-based sensitivity measures** are represented as follows:

$$1 = \sum_i S_i + \sum_i \sum_{j>i} S_{ij} + \dots + S_{12,\dots,k}$$

in this equation,  $S_i, S_{ij}, \dots, S_{12,\dots,k}$  are **Sobol's global sensitivity indices**:

The **first order sensitivity index**  $S_i$  measures and quantifies the sensitivity of model **output Y to the input parameter  $X_i$  (without interaction terms)**, whereas,  $S_{ij}, \dots, S_{12,\dots,k}$  are the sensitivity measures for the higher order terms (interaction terms).

The **total effect sensitivity index**  $S_{Ti}$  measures **the whole effect of the variable  $X_i$** , i.e. the first order effect as well as its coupling terms with the other input variables:

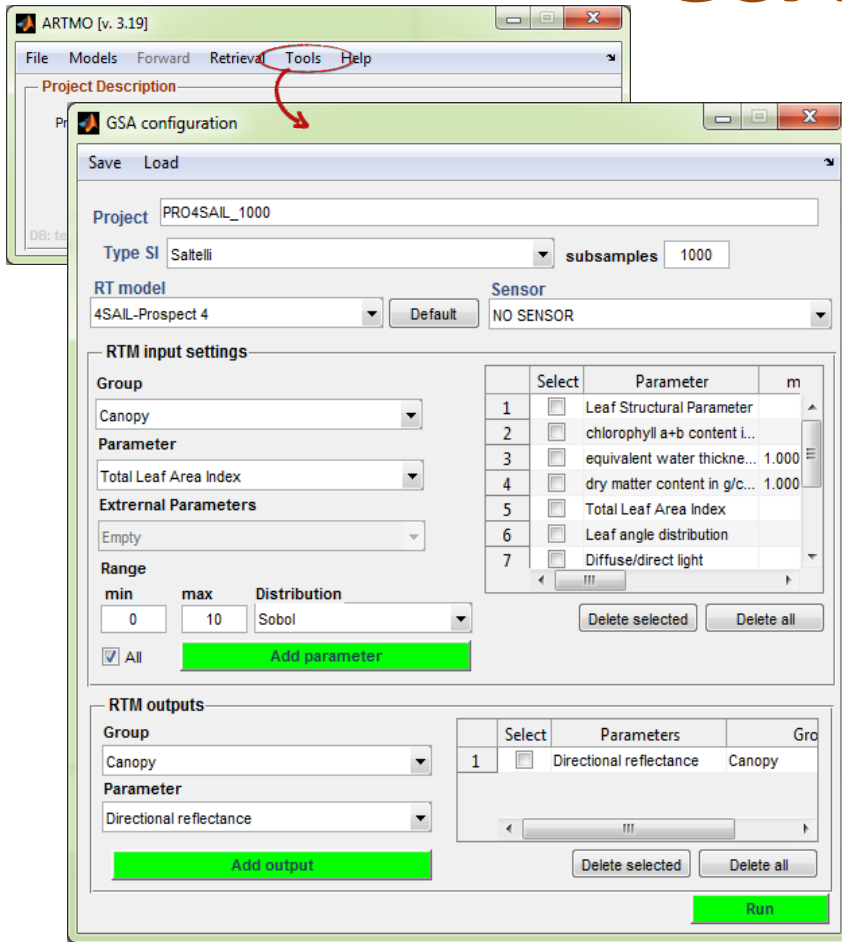
$$S_{T1} = S_1 + S_{12} + S_{13} + S_{123}$$

# GSA toolbox

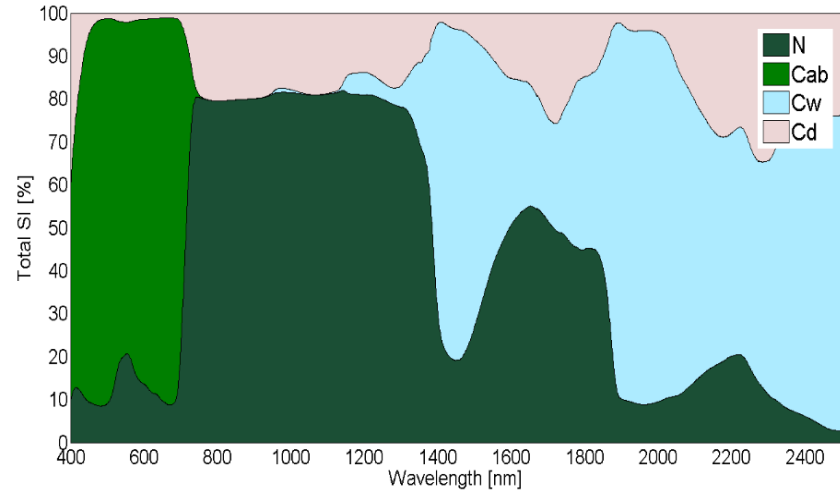
2/2



< 3 min

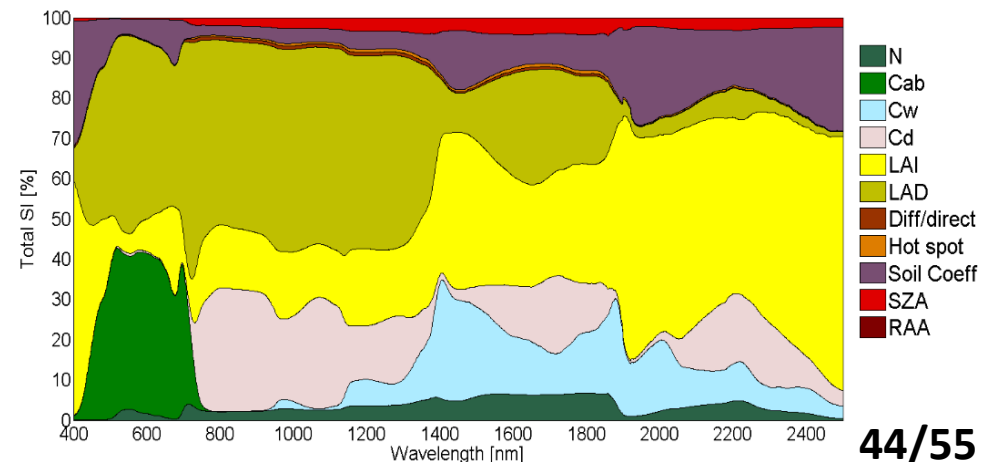


## PROSPECT-4 Reflectance (#1000)



< 5 min

## PROSAIL Directional Reflectance (#1000)

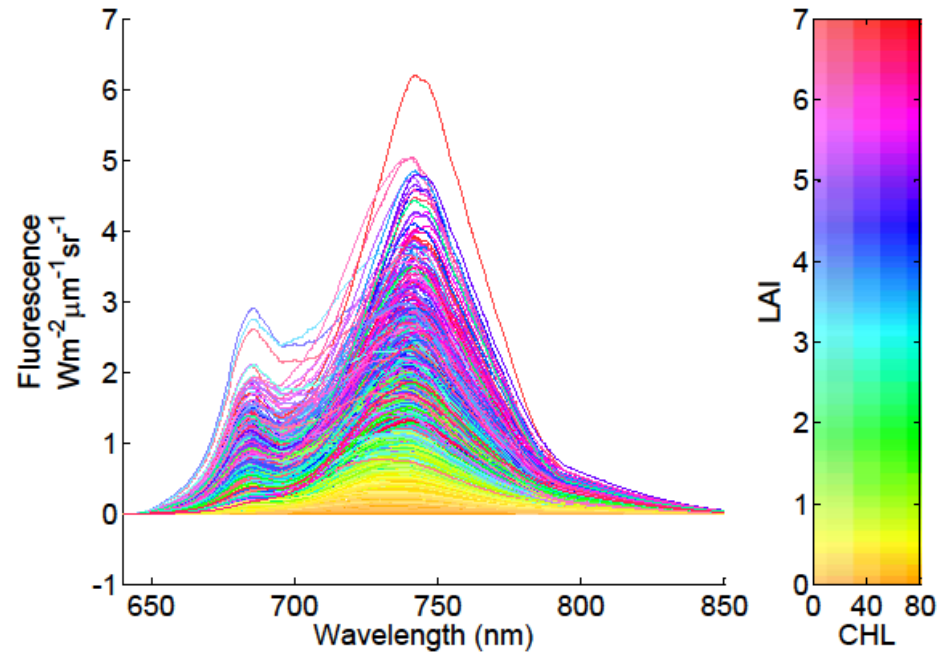


### Properties:

- ARTMO RTMs
- *Saltelli 2010* GSA method
- Various sample distributions
- Results stored in MySQL
- First order or total order Sobol Sensitivity indices
- Can process multiple RTM outputs.

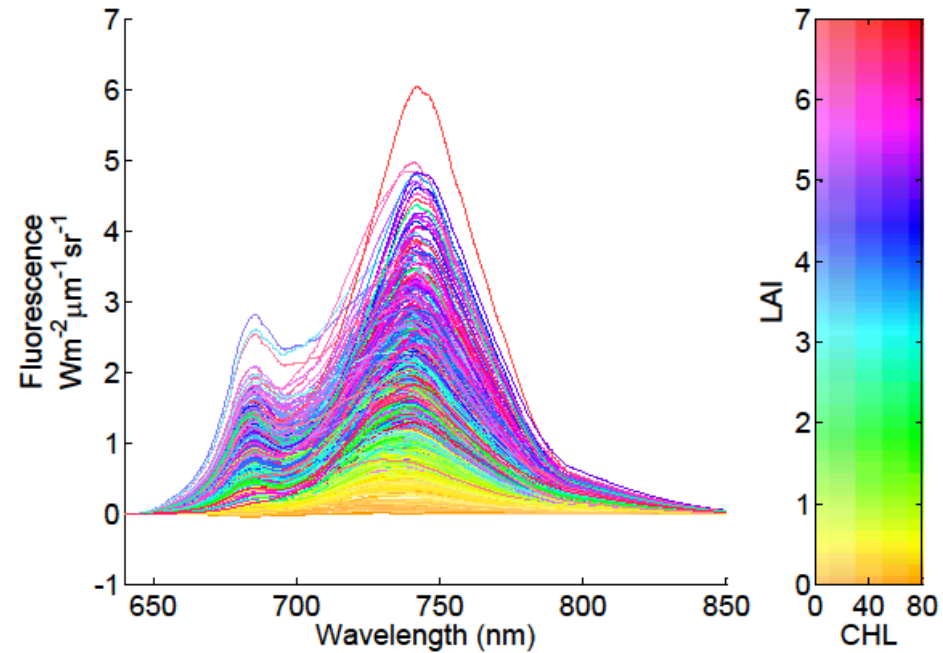
# Any difference?

*Which one would you choose?*



12 min 54 s.

**SCOPE**



1 s.

**Metamodel (emulator)**

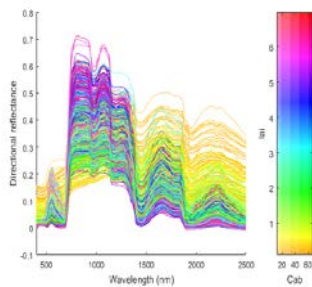


Emulators are regression models that are able to approximate the processing of an RTM, at a fraction of the computational cost:

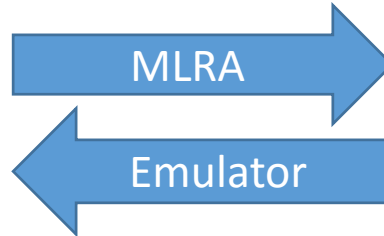
*making a statistical model of a physical model*

## Emulators applied to RTMs:

- In principle any nonlinear, adaptive **machine learning regression algorithms (MLRAs)** can serve as emulators.

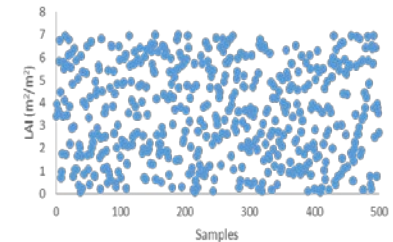


Spectra



Variables

(e.g. LAI, chlorophyll)

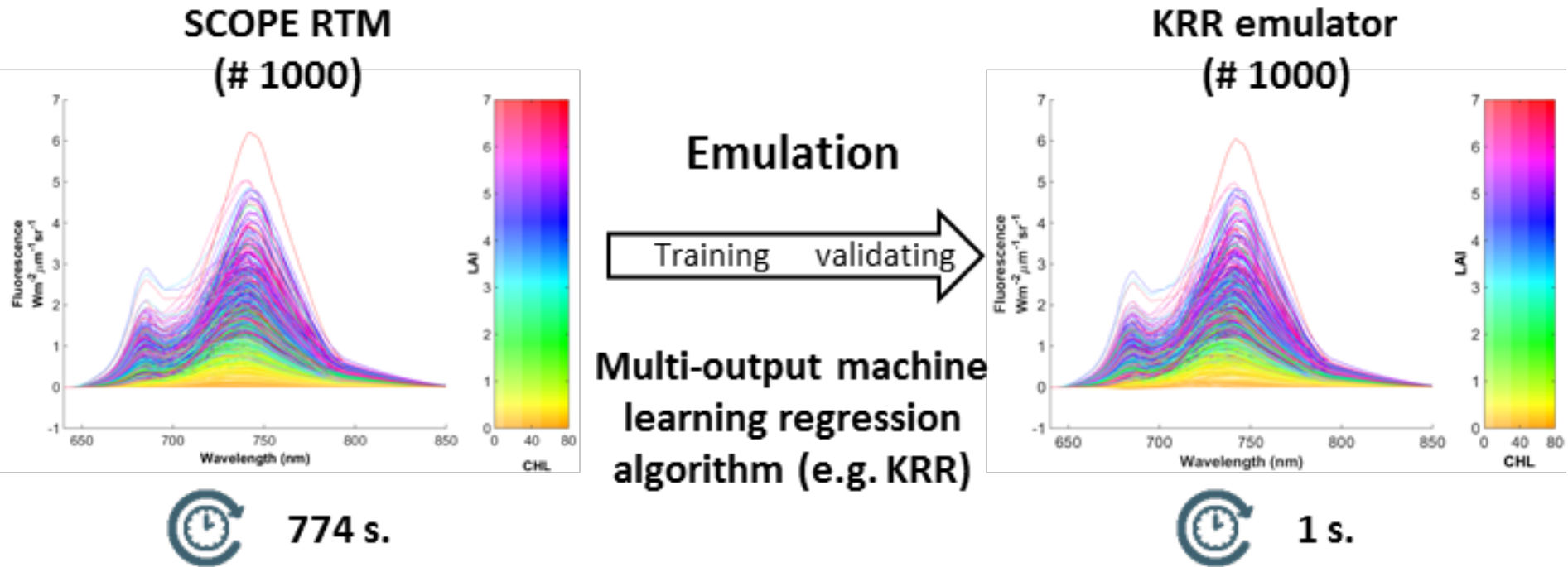


- To emulate RTMs, the emulator should have the capability to reconstruct multiple outputs, i.e. the complete spectrum: resolved with **dimensionality reduction** techniques (e.g. PCA).

## Processing steps:



# Emulating SCOPE fluorescence outputs



Because of the smooth profiles, SIF outputs are easy to emulate.



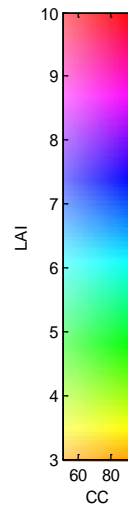
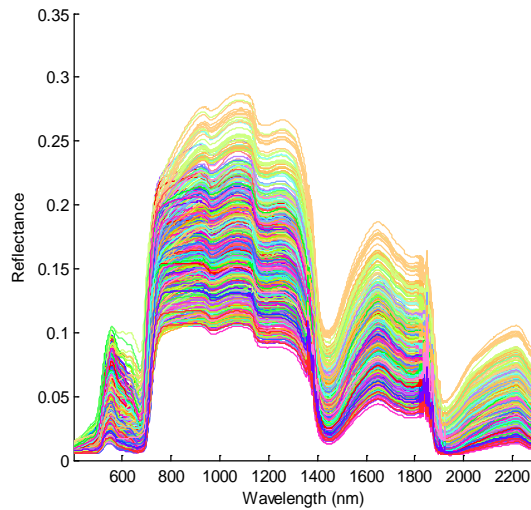
*In Emulation, physical models go hand in hand with machine learning*

# Emulating a complex 3D RTM: DART 4/10

## Experimental setup:

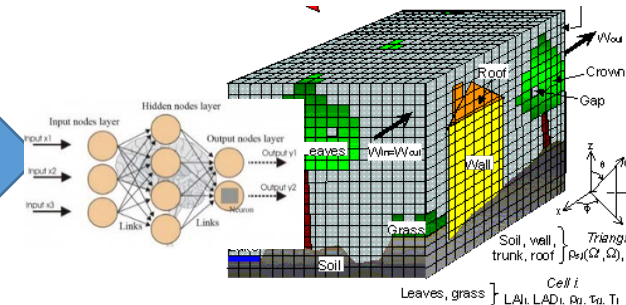
- DART: LUT1000# @ 1 nm; 7 variables
- 3 MLRAs tested: KRR, NN, GPR
- Various # PCA components tested (5, 10, 20, 30)

- N
- LWC
- DMC
- Carc
- LCC
- CC
- LAI
- TOPO



Emulator

- KRR
- NN
- GPR





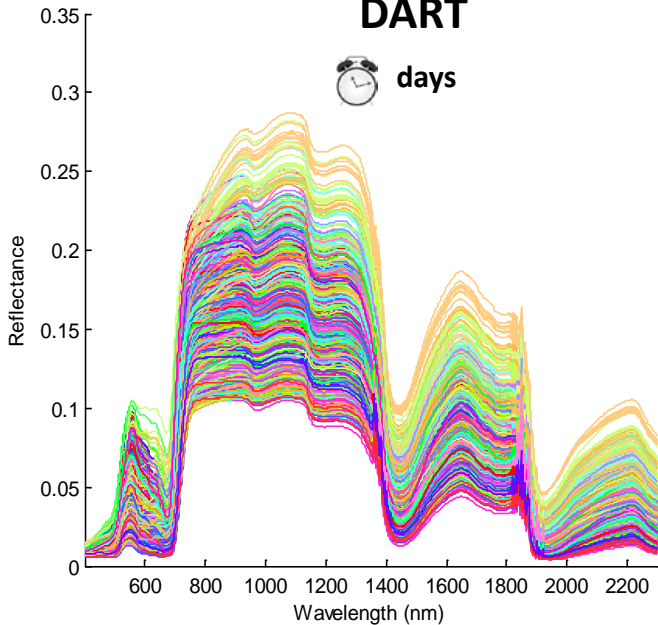
1000#

5/10

**DART**



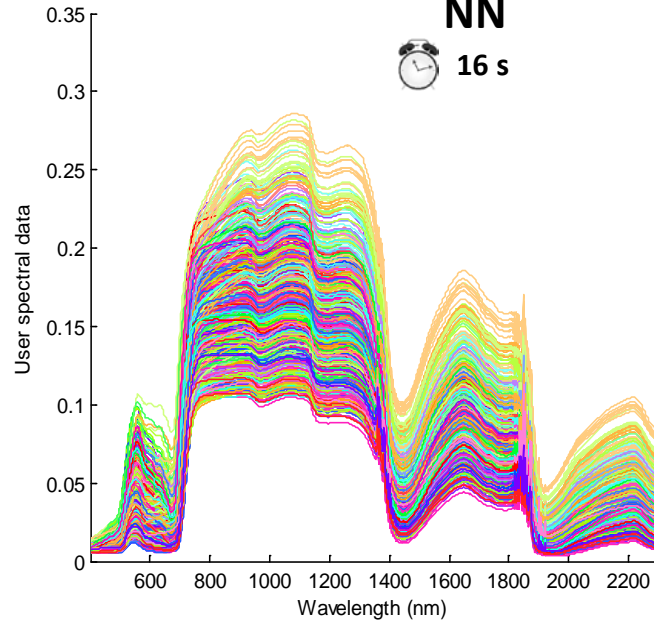
days



**NN**



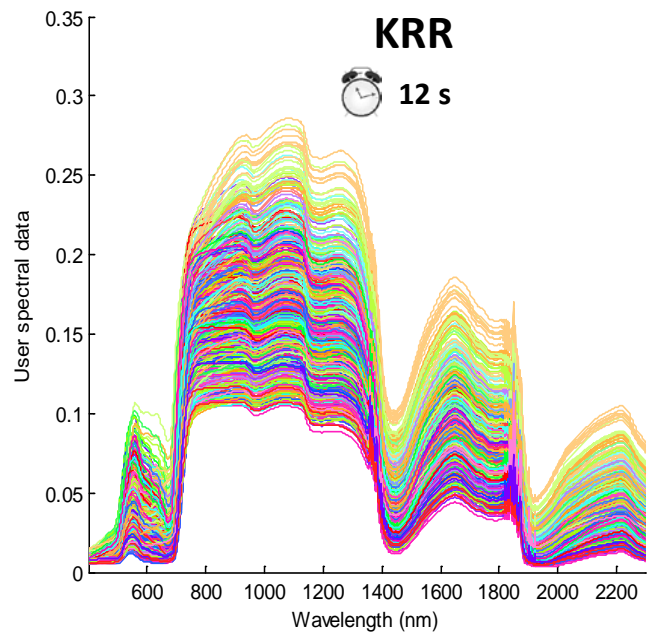
16 s



**KRR**



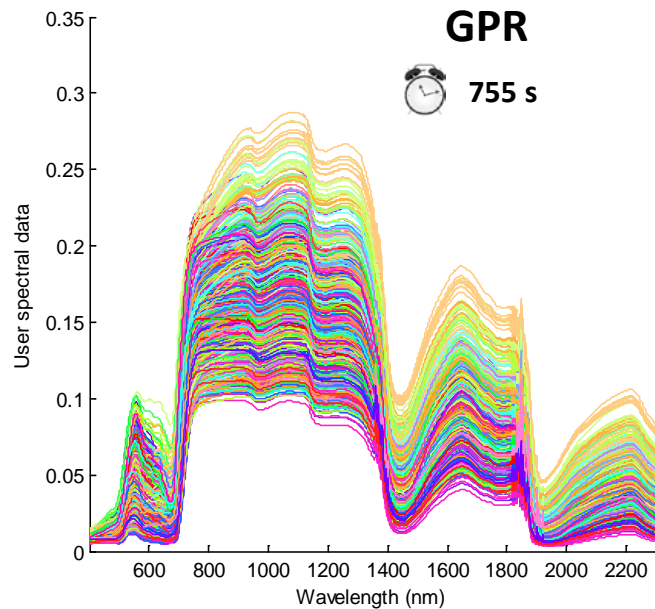
12 s



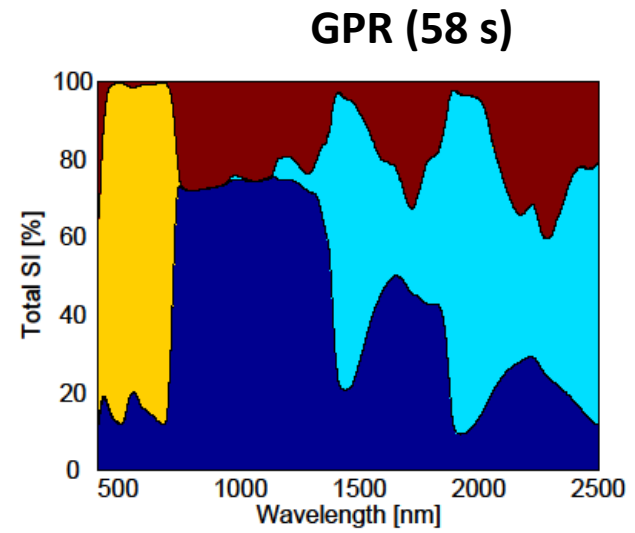
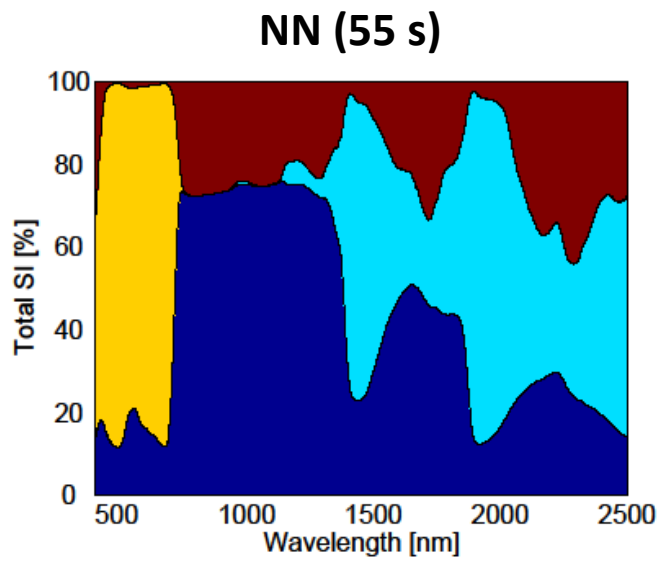
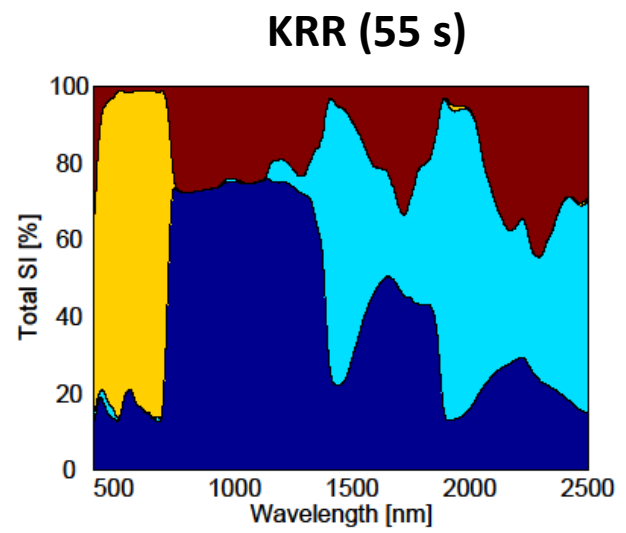
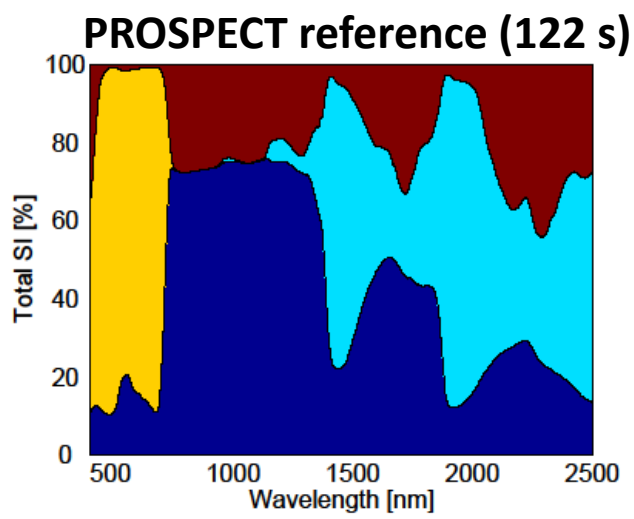
**GPR**



755 s

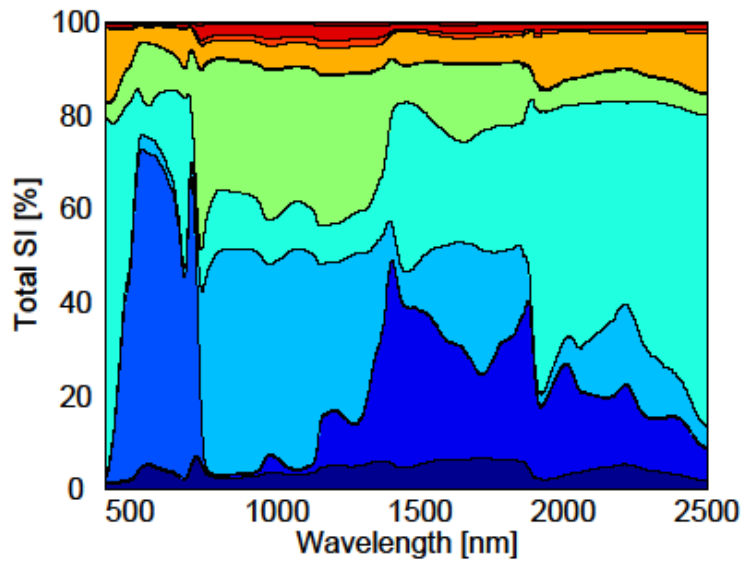


# Emulators applied into GSA: PROSPECT-4

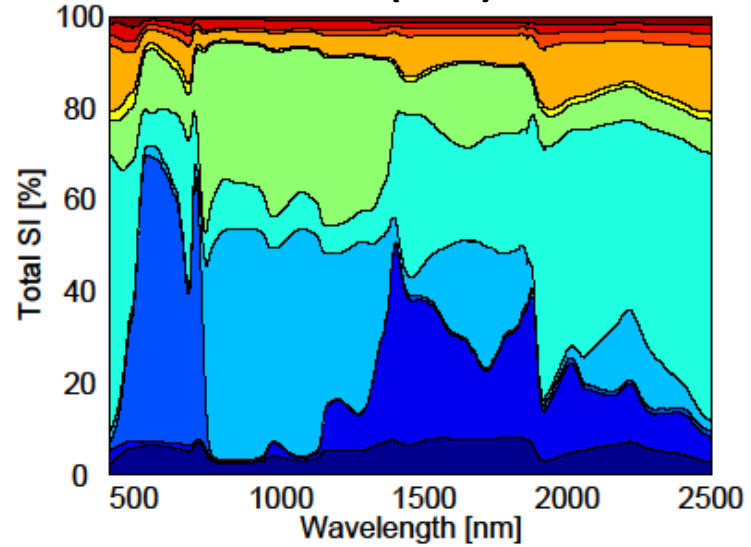


■ N ■ Cw ■ Cab ■ Cm

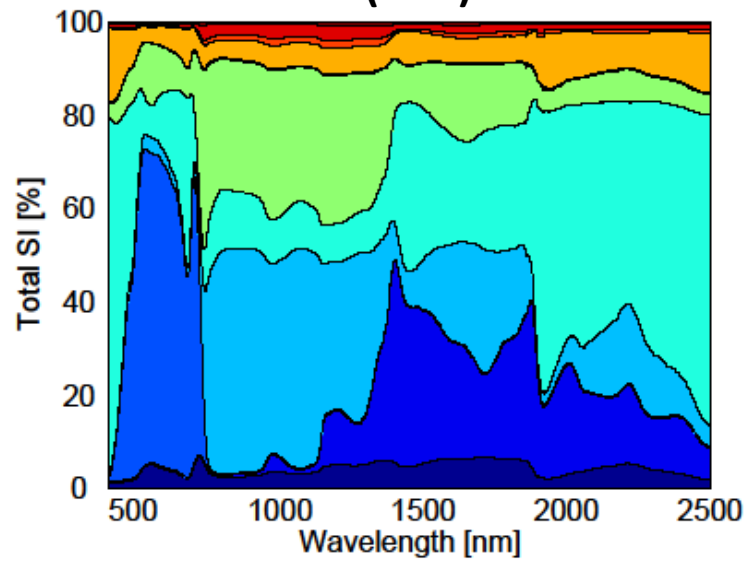
### PROSAIL reference (279 s)



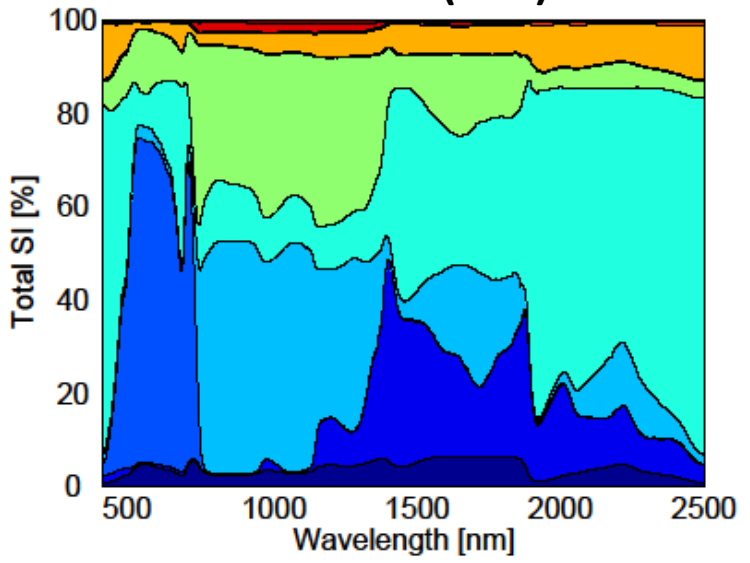
### KRR (73 s)



### NN (80 s)



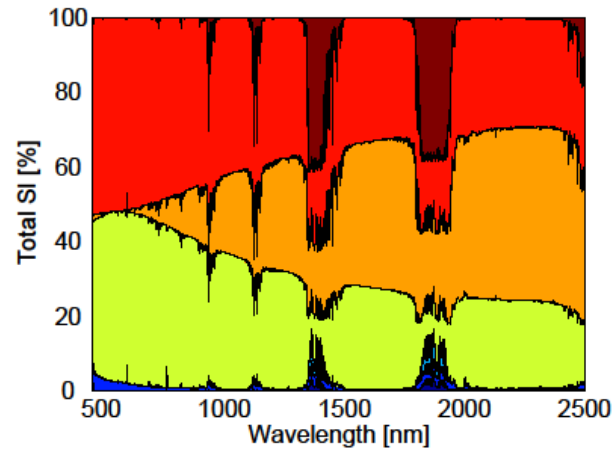
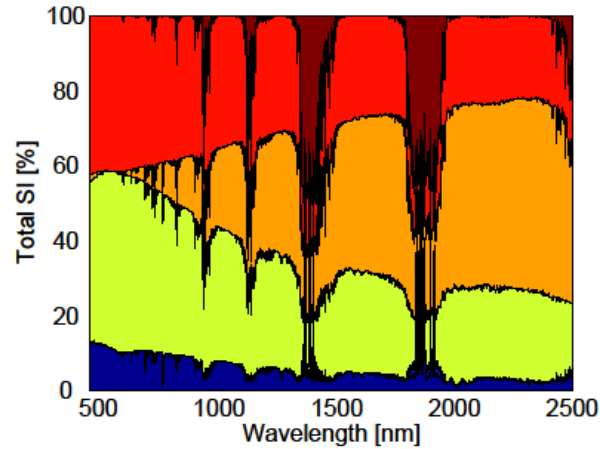
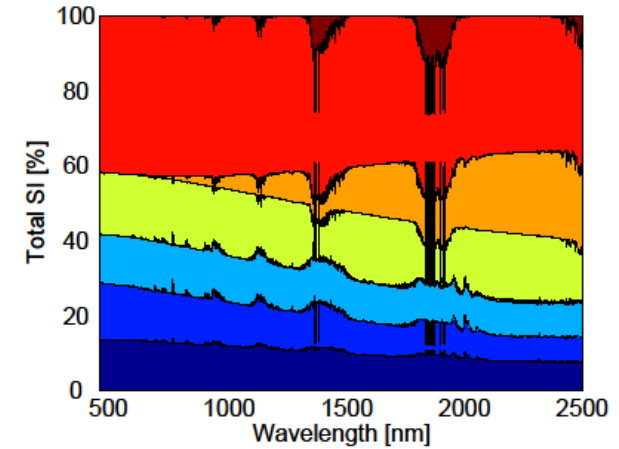
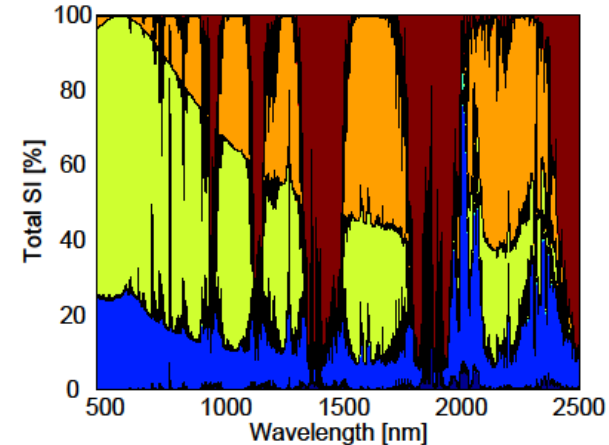
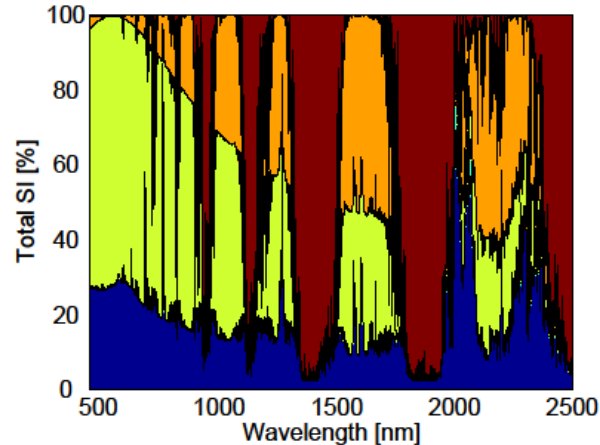
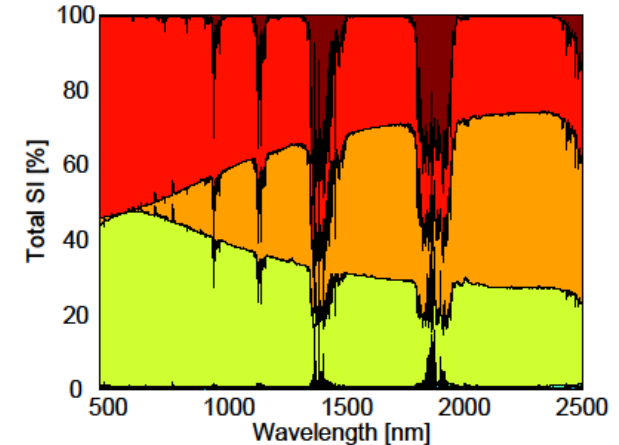
### GPR (79 s)



## MODTRAN

## atmospheric transfer functions:

$$L_{TOA} = L_0 + \frac{(E_{dir}\mu_s + E_{dif})(T_{dif} + T_{dir})\rho}{\pi(1 - S\rho)}$$

 $E_{dif}$  (GPR: 121 s) $T_{dif}$  (NN: 157 s) $L_0$  (GPR: 121 s) $E_{dir}$  (KRR: 101 s) $T_{dir}$  (NN: 151 s) $S$  (GPR: 166 s)

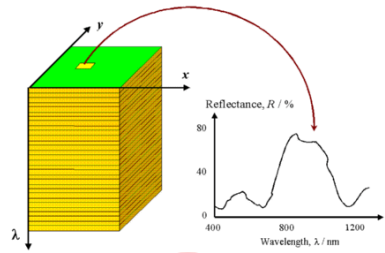
1000#/variable

■ VZA ■ SZA ■ RAA ■ ELEV ■ AOT ■ AMS ■ G ■ CWV

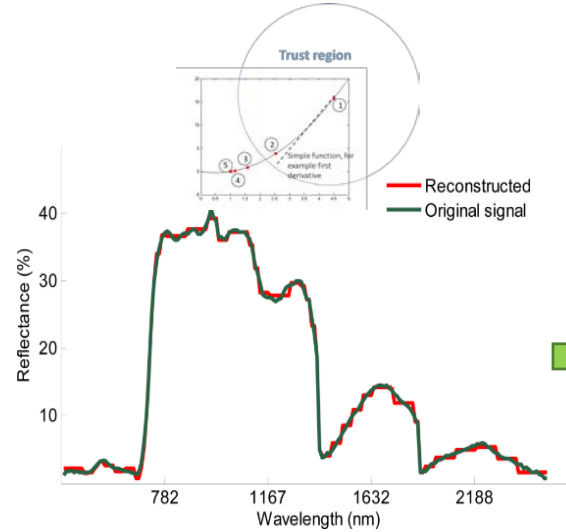
With emulators, processing speed is boosted in the orders of hundred thousand. Using the original MODTRAN simulations would take more than a month.

# Emulators into numerical inversion

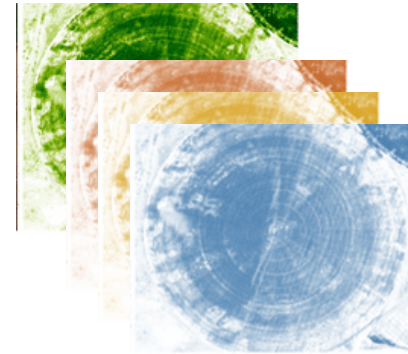
Image



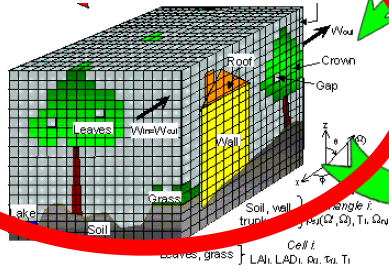
Minimization algorithm: lsqnonlin



Output maps of RTM variables



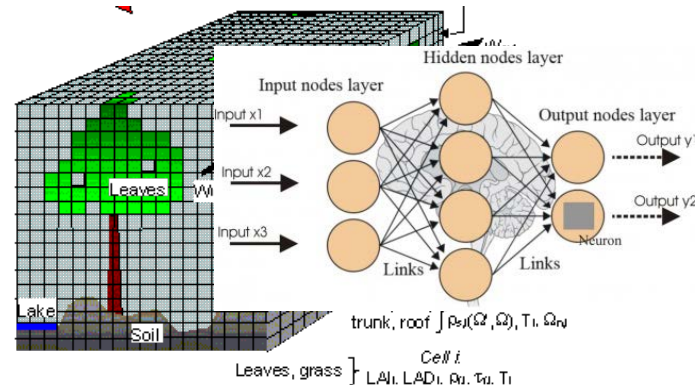
RTM (e.g., DART)

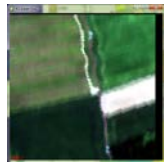


*Per-pixel RTM iterations: very slow method, inapplicable to computationally expensive RTMs.*



Emulation of an RTM





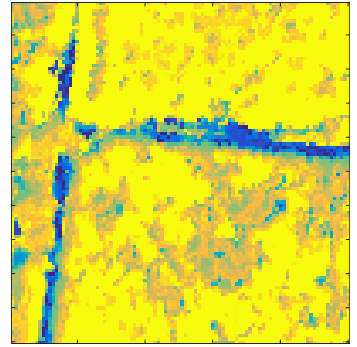
### SCOPE KRR emulator applied to HyPlant DUAL (bare soil spectra added)

 < 1 h

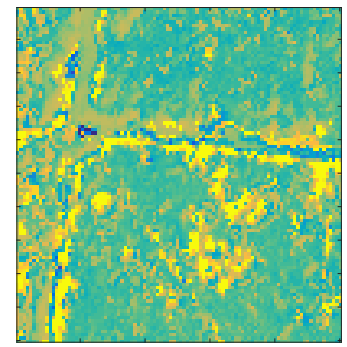
### DART KRR emulator applied to HyPlant DUAL (450-2500 nm)



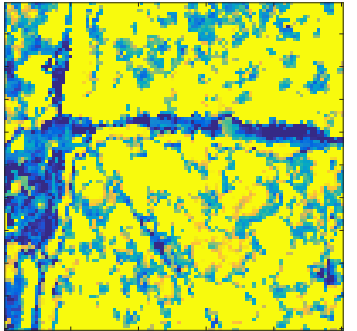
CC



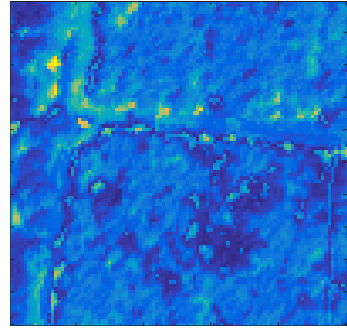
LCC



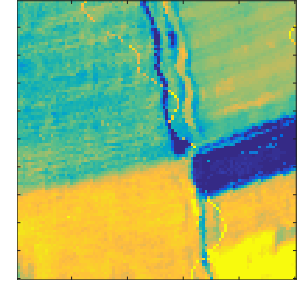
LAI



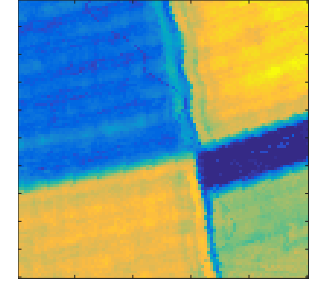
RMSE



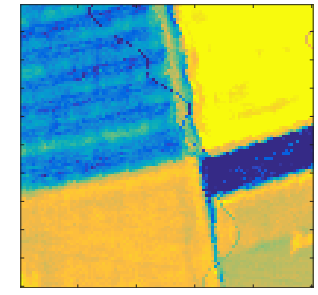
APAR



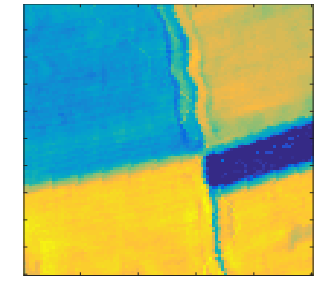
LAI



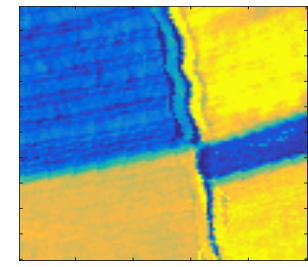
fAPAR



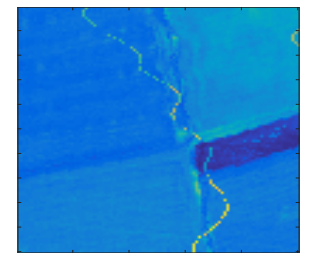
CCC (LCC x LAI)



CWC (Cw x LAI)



RMSE



Retrieval quality depends on : (1) emulator, (2) number and type of included variables.



# Conclusions



Thanks